Numerical characteristics of a centrifugal compressor with a low flow coefficient

Aleksey Yablokov^{1,*}, Ivan Yanin¹, Nikolay Sadovskiy¹, Yuri Kozhukhov¹ and Minh Hai Nguyen²

¹Peter the Great St. Petersburg Polytechnic University, St. Petersburg, Russian Federation

²Petrovietnam exploration production corporation Integrated technical center

Abstract. The study presents the simulation results of the viscous gas flow in low flow coefficient centrifugal compressor stages. The problem is solved in a stationary formulation using the Ansys CFX software package. The numerical simulation is carried out on three ultrahigh-pressure model stages; two stages have blades of the classical type impeller and one stage is of the bodily type. The value of the conditional flow coefficient is 0.0063 to 0.015. As part of the study, block-structured design meshes are used for all gas channel elements, with their total number being equaled as 13–15 million. During the calculations a numerical characteristic was validated with the results of tests carried out at the Department of Compressor, Vacuum and Refrigeration Engineering of Peter the Great St. Petersburg Polytechnic University. With an increase of inlet pressure as a result of a numerical study, it was found that for a given mathematical model the disk friction and leakage coefficient ($1 + \beta_{fr} + \beta_{lk}$) is overestimated. The analysis of flow in labyrinth seals has shown an increase of total temperature near the discs by 30–50 °C, nevertheless this fact did not influence gas parameters in the behind-the-rotor section. The calculation data obtained with finer design mesh (the first near-wall cell was 0.001 mm) is identical to those obtained with the first near-wall cell 0.01 mm mesh.

1 Introduction

Low flow coefficient centrifugal compressors are used to obtain high and ultrahigh gas pressures, which is necessary for modern gas transport systems. So the efficiency increasing of these compressors is an urgent task, especially for the oil and gas industry. The main reason for the efficiency decrease in the low flow stages compressors is the low volumetric flow. And as a result of this are narrow flow sections, small hydraulic diameters, and low Reynolds numbers. This fact was confirmed in works [1, 2, 3], related to the thermo-gas-dynamic principles ultrahigh-pressure centrifugal compressors design and experimental studies. The unsteady nature of the gas flow in the stage of a centrifugal compressor also plays an important role. In the work [4] showed that the amplitude of the pressure change in the peripheral sections of the impeller reaches 4 MPa. According to the results of calculating the unsteady flow in the work [1], a conclusion was made about the undesirability of using traditional design blade diffusers. Low flow rates with small channel sizes require increased manufacturing accuracy and minimal surface roughness, which leads to additional cost increases.

In the work [5], the flow sections losses of a centrifugal compressor are conventionally divided into 5 groups:

- Channel friction losses;

- Vortex loss;
- Secondary losses;
- Losses on internal leakage;
- Loss on disk friction of the outer surfaces of the impellers.

In this article, the authors pay special attention to the 4th and 5th groups, since these losses make up a significant part of all losses in low flow coefficient centrifugal compressor stages.

2 Methods

As an object of study, the authors of the article selected model stages of a ultra-high pressure centrifugal compressor designed, manufactured and tested on a closed-loop stand at the department of the compressor, vacuum and refrigeration Engineering of Peter the Great St. Petersburg Polytechnic University. For model stages, the values of the theoretical flow coefficient lie in the range 0.0063–0.015 and are calculated by the formula:

$$\Phi = \frac{\overline{4m}}{\rho_0^* \pi D_2^2 U_2}, \quad (1)$$

where $\overline{m}$ – mass flow, kg/s; ρ_0^* – inlet gas density, kg/m³; D_2 – outlet diameter of the impeller, m; U_2 – circumferential velocity on the diameter D_2 m/s;

* Corresponding author: yablokovaleksey@mail.ru

Table 1. The number of design mesh elements for numerical models of centrifugal compressor stages.

Name title of the stage	Optimal flow factor Φ_{opt}	Theoretical head factor Ψ_T	Averaged bore, m	The number of rotor blades z_{imp}
Model stage SVD-1	0.083	0.48	0.497	12
Model stage SVD-1	0.08			12

Table 1 presents the main parameters of the model stages SVD-1 and SVD-2 with cylindrical blades.

The model stage of the SVD-6 series has an impeller with body-shaped blades designed with $\Phi_{opt}=0.015$; $\Psi_T=0.545$; $D_{hub} = 0.4$. The number of impeller blades $z_{imp}=8$. The impeller SVD-6 was designed so that the equivalent opening angle of the channels does not exceed 10 degrees. The channels, as well as the outer surfaces of the SVD - 6 disks, have a roughness $Ra = 5 - 2.5$. The return channel middle line blades are made along an arc of a circle. The blade angle at the exit of the return channel is 90° , and at the entrance is 25° . The number of blades is 16. A vaneless diffuser with $D_4/D_2 = 1.55$ is installed in the stage. Figure 1 shows the schematic diagram of the SVD-6 intermediate stage rotor.

Fig. 1. A schematic diagram of the SVD-6 intermediate stage rotor.

The numerical simulation of the viscous gas flow in the model stages SVD channels was carried out in the

Ansys CFX software package in a stationary formulation with a subsonic gas flow. The flowing gas channels centrifugal compressor stage model was the volume enclosed between the bounding surfaces of the real stage. This volume was completely filled with a block-structured grid. The number of elements of the computational grid of model stages, rounded to thousands, is given in Table 2. Various boundary conditions were set on the model surfaces. The numerical study model consists of the elements shown in Figure 2.

Fig. 2. A gas channel schematic diagram of the stage in meridional plane: 1 – inlet guide; 2 – rotor; 3 – vaneless diffuser; 4 – crossover; 5 – return channel; 6 – output guide; 7 – labyrinth seals along the covering disc; 8 – labyrinth seals along the main disc.

Table 2. The number of design mesh elements for numerical models of centrifugal compressor stages.

№	Name title of the stage	Total number of elements, mln	Number of impeller elements, mln
1	Model stage SVD-1	15 700 000	3 000 000
2	Model stage SVD-2	14 000 000	2 800 000
3	Model stage SVD-6	13 000 000	2 500 000

Table 3. Input parameters for designing of model stage.

№	Name title of the stage	Inlet pressure, MPa	Gas type
1	Model stage SVD-1	0.1	Air ideal gas
		0.41	Nitrogen N2
		1.0	Nitrogen N2
2	Model stage SVD-2	0.1	Air ideal gas
		0.41	Nitrogen N2
		1.0	Nitrogen N2
3	Model stage SVD-6	0.1	Air ideal gas
		0.41	Nitrogen N2
		1.0	Nitrogen N2
		2.0	Nitrogen N2

Table 3 shows the boundary condition parameters at the entrance to the computational domain. Mass flow was set at the exit from the calculation area. It was calculated by the input parameters through the conditional flow coefficient Φ .

The SST turbulence model was used for all low flow stage models. The value of the near-wall function y^+ is less than 3. The calculated block-structured grids were designed according to the recommendations of the authors of the works [6-18]. The results of the work were obtained using computational resources of Peter the Great Saint-Petersburg Polytechnic University Supercomputing Center (www.spbstu.ru).

3 Results and Discussion

The methodology of the Department KViHT was used to process the results of a numerical study and the following main parameters were calculated:

1. The conditional flow coefficient:

$$\Phi = \frac{\overline{4m}}{\rho_0^* \pi D_2^2 U_2} \quad (2)$$

The polytropic pressure coefficient:

$$\psi_p = \frac{h_p}{U_2^2} \quad (3)$$

where h_p - polytropic head, J/kg;

2. The coefficient of polytropic head with the difference of the kinetic energies of the gas:

$$\psi_p^* = \frac{h_p^*}{U_2^2} \quad (4)$$

3. The coefficient of internal head:

$$\psi_i = \frac{h_i}{U_2^2} \quad (5)$$

$$h_i = \frac{N_i}{U_2^2} \quad (6)$$

where h_i - internal head, J/kg; N_i - engine power transmitted to the gas by the impeller of the stage, N/m².

For the case of insignificant influence of heat transfer, the calculation is carried out according to the formula:

$$h_i = i_0^* - i_0^* \quad (7)$$

4. Polytropic efficiency by static parameters:

$$\eta_p = \frac{h_p}{h_i - h_d} \quad (8)$$

5. Polytropic efficiency by complete parameters:

$$\eta_p^* = \frac{h_p^*}{h_i} \quad (9)$$

6. Power friction with the friction torque

$$N_{fr} = \omega \cdot M_{fr} = k_{fr} \rho U_2^3 D_2^2 \left(1 - \frac{D_1^2}{D_2^2}\right) \cdot 10^{-6} \quad (10)$$

where $k_{fr} = \pi \lambda_1 \cdot 10^2$ - coefficient dependent on

Reynolds number $Re_u = \frac{U_2 D_2}{2\nu_2}$, surface roughness of the

disk and relative to the lateral clearance $\frac{b_2}{D_2}$ between the disk and the housing, determined according to Tsumbush.

Figures 3, 4 show the characteristics of the model stage SVD - 1 according to the results of a numerical study in comparison with the experimental results. The calculated input pressure is 0.1 MPa of air ideal gas. The characteristics are built in section 2-2.

Fig. 3. Estimated and experimental characteristics of SVD-1 stage at $Re_u = 2.5 \cdot 10^6$ in section 2-2. Inlet pressure $P = 0.1$ MPa, actuating medium – ideal gas.

Fig. 4. Estimated and experimental characteristics of cumulative leak and disk friction loss factor ($1 + \beta_{fr} + \beta_{lk}$). Inlet pressure $P = 0.1$ MPa, actuating medium – ideal gas.

Figures 5 show the calculated and experimental characteristics of the SVD-1 stage with an inlet pressure

of 0.4 MPa. A real nitrogen gas model was used to simulate a viscid gas flow.

Fig. 5. Estimated and experimental characteristics of SVD-1 stage at $Re_u=1 \cdot 10^7$ in section 2-2; Inlet pressure $P = 0.4$ MPa, actuating medium – nitrogen.

Figures 6, 7 show the calculated and experimental characteristics of the SVD - 1 at an inlet pressure of 1 MPa. Calculation at an inlet pressure of 1 MPa was carried out taking into account the roughness; the equivalent sand roughness was set.

Fig. 6. A comparison of experimental characteristic of SVD-1 stage at $Re_u=2,5 \cdot 10^7$ with estimated in section 2-2. Inlet pressure $P = 1$ MPa, actuating medium – nitrogen.

Fig. 7. Estimated and experimental characteristics of cumulative leak and disk friction loss factor ($1+\beta_{fr}+\beta_{lk}$). Inlet pressure $P = 1$ MPa, actuating medium – nitrogen.

Figures 8 show the characteristics of the model stage SVD – 2 according to the results of a numerical study in comparison with the experimental results. The calculated input pressure is 0.1 MPa of air ideal gas. The characteristics are built in section 2-2.

Fig. 8. Estimated and experimental characteristics of SVD-2 stage in section 2-2.

Figure 9 show the characteristics of the model stage SVD – 2 according to the results of a numerical study in comparison with the experimental results. Inlet pressure $P = 0.4$ MPa, actuating medium – nitrogen.

Fig. 9. Estimated and experimental characteristics of SVD-2 stage in section 2-2. Inlet pressure $P = 0.4$ MPa, actuating medium – nitrogen.

Figure 10 show the characteristics of the model stage SVD – 2 according to the results of a numerical study in comparison with the experimental results. The calculated inlet pressure is 0.1 MPa of air ideal gas. The characteristics are built in section 2-2.

Fig. 10. Estimated and experimental characteristics of SVD-6 stage in section 2-2. Inlet pressure is 0.1 MPa of air ideal gas.

Figure 11 show the characteristics of the model stage SVD – 6 according to the results of a numerical study in comparison with the experimental results. Inlet pressure $P = 2$ MPa, actuating medium – nitrogen.

Fig. 11. Estimated and experimental characteristics of SVD-6 stage in section 2–2.. Inlet pressure $P = 2$ MPa, actuating medium – nitrogen.

4 Conclusions

The study showed that in the viscid gas flow numerical simulation of low flow coefficient stages exist features which are related to an overestimation of the pressure characteristic for the flow rates greater than the nominal in atmospheric inlet pressure conditions. However, the opposite effect was obtained for the SVD-2 stage. The pressure curve and the efficiency curve will change when the domain of the vaneless diffuser is rotated with the walls braking to zero.

It is expected that under atmospheric input conditions, this approach will make it possible to bring the calculated characteristics closer to the experimental ones.

Also, during the study, it was found that the curve of the total loss coefficient for leaks and disk friction ($1 + \beta_{fr} + \beta_{lk}$) for SVD-1 under atmospheric input conditions is very close to the experimental curve. But the calculated characteristic increased by 5–7% for other input conditions. This is possibly explained by differences in the roughness of the surfaces of the model and the real object (the equivalent sand roughness was set for numerical investigation).

The size of the computational grid in seals minimally affects the results of a numerical study. The same results were obtained when the size of the first parietal cell was 0.001 and 0.01 mm. Also, a temperature increase of up to 50°C in the labyrinth seals near the impeller walls was noted in the calculation. But it does not overestimate the temperature values in the section behind the impeller and does not cause an artificial increase in the internal head of the stage. This temperature grows in the stage seals can be caused by the energy supply from the rotating disk. While in the real impeller flow this is not possible. In general, the simulation results of the SVD stages characteristics are very similar with the real

characteristics when using nitrogen with input conditions of 0.4; 1.0 and 2.0 MPa.

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