

## Modelling of simple shear tests on volcanic unsaturated sands

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**Abstract.** In landslide susceptibility analysis, a relevant issue is the proper modelling of the complex mechanisms that regulate the failure and post-failure stages. In this paper, simple shear experiments replicating the kinematics of failure in landslide-prone areas are interpreted through an elastoplastic strain-hardening constitutive model for both saturated and unsaturated soils. The material tested is an air-fall volcanic (pyroclastic) soil from Southern Italy which originated from the explosive activity of the Somma-Vesuvius volcanic apparatus. Data from triaxial and shear tests performed on remoulded specimens characterized by saturated and unsaturated conditions are used to calibrate the model parameters. The evolution of shear stress, volumetric and shear strain measured during the experiments are reproduced by means of a model formulation specific for simple shear conditions. To capture the strength emerging under different states of saturation, non-associated flow rule, and a suction-dependent yield surface are used. Examination of the experimental data available for various testing conditions enabled the quantification of the variability of fundamental model constants, such as those controlling frictional resistance and water retention behaviour. To account for such scatter in the physical properties, the constitutive analyses are performed by employing varying model constants within a band of admissible values. The resulting model performance is validated by comparing the simulations with the experimental results at different saturation conditions. The results show that the combination of the proposed model with a data-driven determination of the range of variation of hydro-mechanical properties is crucial to satisfactorily simulate the essential features of the soil response under a variety of simple shear testing regimes.

### 1 Introduction

The occurrence of rainfall-induced shallow landslides of the flow-type has posed great threats to densely populated regions due to its long-travel distance and high runout velocity [1]. Massive events have been recorded in unsaturated pyroclastic deposits in Southern Italy, where the activities of Somma-Vesuvius volcanic system have produced vast amounts of pyroclastic soil along steep slopes. Upon wetting, the suction drop within the unsaturated regime weakens the soil, thus increasing its potential to experience shear failure and move downslope through a rapid flow process [2]. For this reason, experimental and numerical tools are highly needed to identify the material properties responsible for such dramatic failures, as well as to estimate the regional landslides susceptibility [3, 4].

Recently, a range of laboratory experiments based on triaxial and shear configurations have been carried out on samples obtained from the Sarno-Quindici area to clarify the mechanical characteristics of the pyroclastic soils. Specifically, the simple shear devices have been improved to extend their use to partially saturated soils [5] and multiple loading sequences have been investigated to mimic the in-situ conditions of the shallow slopes. The pyroclastic soils were generally categorized as coarse-grained materials and tested under both saturated and unsaturated conditions. The simple shear tests on saturated samples

normally experience the contractive processes, while on unsaturated samples display a transition from contractive to dilative response [6].

Quantifying such transitions, as well as their role in triggering flow instabilities, requires effective constitutive relationships able to cope with a varying degree of saturation. This paper discusses a modeling strategy aimed at combining such recent experimental data with an advanced constitutive model for pyroclastic soils. Specifically, the following sections make reference to simple shear testing conditions, with the purpose to constrain the range of admissible model constants leading to accurate numerical simulations under both saturated and unsaturated regimes. Special attention is given to the variation of the soil properties and its effect on the model performance by allowing the parameters to vary within a range defined from the scatter of the experimental data. For simplicity purpose, the scope of the analysis has been restricted to the parameters that control the frictional resistance, and those describing the soil water retention curve (SWRC), with the ultimate goal to ascertain whether such simple steps are sufficient to lead to satisfactory simulations.

### 2 Constitutive model

Due to the multiphase interactions among the solid, fluid, and gas phases constituting an unsaturated soil, quantifying the stress state acting on the solid skeleton requires

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special treatments. In this context, a particular stress measure often used to quantify the skeleton stress is the so-called Bishop effective stress [7–9], expressed as follows:

$$\sigma'_{ij} = \sigma_{ij} - u_a \delta_{ij} + S_r s \delta_{ij} \quad (1)$$

where  $S_r$  and  $s$  are degree of saturation and suction, respectively, while  $\sigma_{ij}$  is the total stress,  $u_a$  is the pore air pressure, usually assumed constant and equal to the atmospheric pressure, and  $\delta_{ij}$  is the Kronecker delta. The relationship between  $S_r$  and  $s$  is defined by the SWRC and generally interpreted with the van Genuchten retention model [10]:

$$\theta(s) = \theta_r + \frac{(\theta_s - \theta_r)}{\left[1 + (\alpha_{vg} s)^{n_{vg}}\right]^{m_{vg}}} \quad (2)$$

where  $\theta$  is the volumetric water content,  $\theta_r$  and  $\theta_s$  are its values at residual and saturated conditions, and  $\alpha_{vg}$ ,  $n_{vg}$  and  $m_{vg} = 1 - 1/n_{vg}$  are shape parameters.

For coarse-grain materials like pyroclastic soils, a frictional relation is often used to define the yielding conditions [11]:

$$f = \tau - \eta_Y \sigma' \quad (3)$$

where  $\eta_Y$  is the stress ratio at yielding,  $\tau$  is the shear stress and  $\sigma'$  is the effective normal stress. And as indicated experimentally, the unsaturated samples have the possibility to experience the transition from contractive to dilative responses. For this reason, to account for the role of density on the volume change of variably saturated pyroclastic soil samples, the concept of state parameter  $\psi$  [12, 13] is introduced into a non-associated flow rule by adjusting the dilatancy function proposed by Lagioia et. al. [14], as follow:

$$D = \frac{d\varepsilon_p}{d\gamma_p} = \mu_g (M_g^* - \eta) \left( \frac{\alpha_g M_g^*}{\eta} + 1 \right) \quad (4)$$

$$M_g^* = M_g \exp(m_g \psi)$$

where  $\mu_g$ ,  $m_g$ , and  $\alpha_g$  are shape parameters and  $M_g$  is the critical stress ratio governed by the friction angle  $\varphi$  (i.e.,  $M_g = \tan(\varphi)$ ). In the above equation, the state parameter  $\psi$  is defined as the difference between the current porosity  $n$  and the critical state porosity  $n_{cs}$ . Specifically, since the state parameter  $\psi$  quantifies the distance between current state and the critical state line (CSL) in the  $n$ - $\log \sigma'$  space, its introduction into the constitutive relationship makes the model porosity-dependent. Furthermore, since evidence available in the literature suggests that suction causes an upward shift the CSL [15], the state parameter can be augmented by incorporating suction into its definition, as follows:

$$\psi = n - n_{cs} (1 + bs), \quad n_{cs} = N_{cs} - \lambda_{cs} \ln \sigma' \quad (5)$$

where  $N_{cs}$  and  $\lambda_{cs}$  represent the intercept and slope of the CSL in the  $n$  -  $\log \sigma'$  space corresponding to fully saturation, and  $b$  reflects the effects of  $s$  on the CSL.  $\varepsilon$  and  $\gamma$  are the normal and shear strains, respectively, with the

superscript  $p$  representing their plastic portions, computed as:

$$d\varepsilon^p = \Lambda \frac{D}{\sqrt{1 + D^2}}, \quad d\gamma^p = \Lambda \frac{1}{\sqrt{1 + D^2}} \quad (6)$$

where  $\Lambda$  is the plastic multiplier derived from the consistency condition. The hardening law is defined as:

$$d\eta_Y = (M_p - \eta_Y) \frac{1}{\lambda} d\gamma_p \quad (7)$$

where  $\lambda$  is a hardening constant and  $M_p = M_g$  for simplicity. Furthermore, the elastic responses are captured by hypoelasticity with the Young's modulus  $E$  and shear modulus  $G$  expressed as:

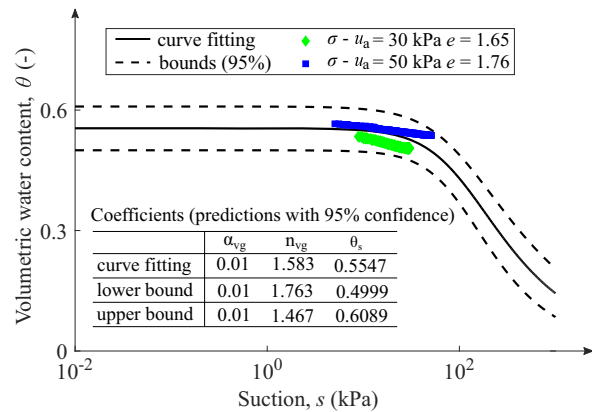
$$E = E_r \left( \frac{\sigma'}{\sigma_r} \right)^{n_E}, \quad G = G_r \left( \frac{\sigma'}{\sigma_r} \right)^{n_G} \quad (8)$$

where  $n_E$  and  $n_G$  are constant power law coefficients;  $E_r$  and  $G_r$  are the values of the elastic moduli at the reference stress  $\sigma_r$  (normally being 1 kPa).

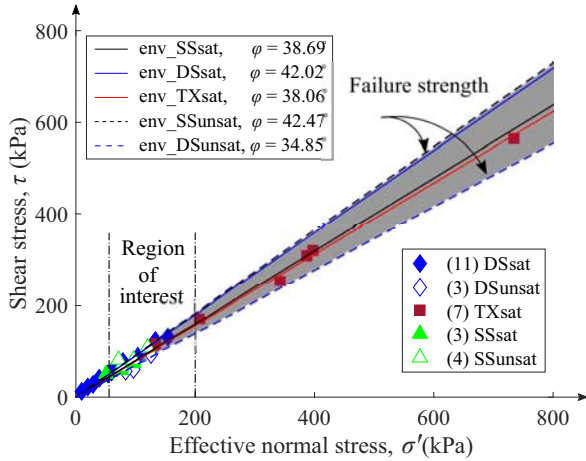
### 3 Calibration procedure

The model parameters were calibrated based on the experimental data available for the pyroclastic soil derived from the explosive activity of the Somma-Vesuvius volcanic apparatus (Southern Italy). The experimental data on remolded specimens are used to illustrate the model calibration procedure.

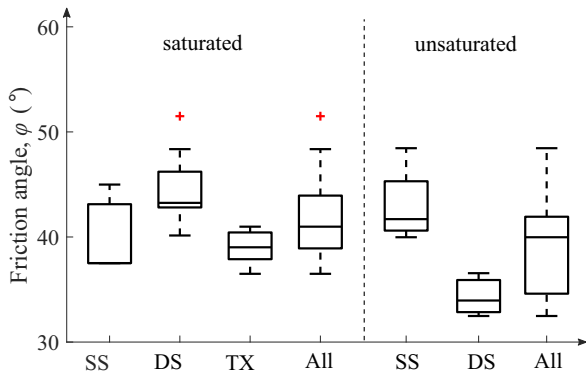
Parameters related to the SWRC were calibrated using two wetting tests under simple shear conditions. The tests were performed at constant normal stress (30 and 50 kPa) and constant shear stress (34 and 51 kPa), and the suction was zeroing with a fixed rate of 0.1 kPa/h. The SWRCs are extracted from the wetting tests considering only the part at constant and low shear strain ( $\gamma \approx 0.05$ ). Figure 1 illustrates the experimental data along with the calibrated van Genuchten retention model. The figure also illustrates the estimated upper and lower bounds of the water retention curve, here defined to encompass the 95% confidence



**Figure 1.** Calibration of the SWRCs interpolated using the van Genuchten model. Dashed lines represent the prediction bounds for a new observation with 95% confidence level. And the table lists the values of the fitting coefficients with  $\theta_r = 0.0002$ .



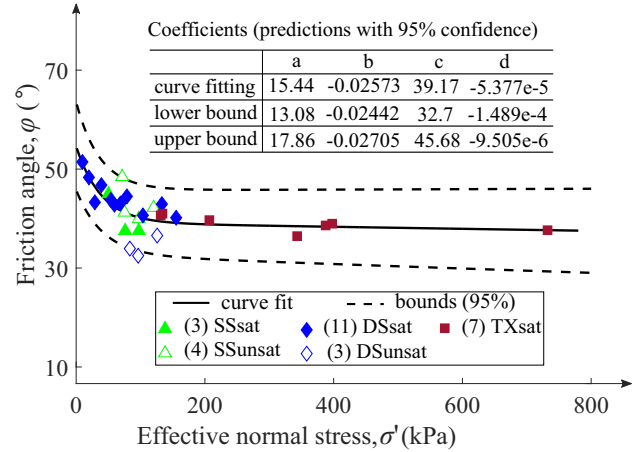
**Figure 2.** Shear strength envelope determined through Simple Shear tests (SS), Direct Shear tests (DS) and Triaxial tests (TX) on saturated and unsaturated specimens (SS, TX and DS data is taken from [16], [17] and [18]). The numbers in the brackets are the number of tests considered to obtain shear strength envelopes; the region of interest represents the range of effective stress investigated using numerical simulation.



**Figure 3.** Variability of  $\varphi$  under various testing protocols.

interval associated with the available data (dashed lines in Figure 1). The fitting coefficients ( $\alpha_{vg}$ ,  $\theta_s$  and  $n_{vg}$  with  $\theta_r = 2e^{-5}$ ) are reported in Figure 1.

The critical stress ratio  $M_g$  is calibrated on the basis of the results obtained with three different testing devices, including Direct Shear (DS), Simple Shear (SS) and Triaxial (TX) apparatus, under various saturation conditions, as shown in Figure 2 [16]. The list of tests considered is reported in Table 1. Five shear strength envelopes specified for different testing conditions are obtained through a linear fitting with no cohesion and the friction angle is evaluated for each test as  $\varphi = \arctan(\tau/\sigma')$ . The results readily illustrate the variability of the friction angle  $\varphi$  under different testing conditions. To further illustrate the variability of  $\varphi$ , Figure 3 describes the distribution of  $\varphi$  for each of the imposed testing regimes through maximum, minimum, mean first and fourth quantile. Comparisons between saturated and unsaturated samples indicate that the presence of suction is responsible for an additional variation in the friction properties. Therefore, a relationship between friction



**Figure 4.** Relationship between friction angle and effective normal stress. Dashed lines represent the prediction bounds associated to 95% confidence level.

angle ( $\varphi$ ) and effective normal stress ( $\sigma'$ ) is established to account for the stress-dependent failure strength as represented in Figure 4. An exponential expression is used to obtain the best fit between  $\sigma'$  and  $\varphi$ , which is expressed as:

$$\varphi(\sigma') = a \cdot \exp(b \cdot \sigma') + c \cdot \exp(d \cdot \sigma') \quad (9)$$

where  $a$ ,  $b$ ,  $c$ , and  $d$  are fitting parameters and their values are listed in Fig. 4. Despite the good agreement with the measured trends illustrated in Fig. 4, the large data scatter resulted into an  $R^2 = 0.51$ . Thus, similar to the variability in SWRC, the prediction bounds for a new observation with 95% confidence level are also provided in Figure 4 to quantify the uncertainty in estimating  $\varphi$  and the fitting coefficients are summarized in Figure 4. In the following sections, their role will be studied with reference to simple shear tests conducted under both saturated and unsaturated conditions.

The critical state parameters  $N_{cs}$  and  $\lambda_{cs}$  have been constrained in the  $n$ -log  $\sigma'$  plane. Since none of the TX, DS and SS tests fully reached the critical state, the precise determination of the location of the Critical State Line (CSL) was not possible. Hence, approximately, the CSL is evaluated by hypothesizing that the Critical State is reached at large deformations (e.g. for TX tests it was supposed that CSL was reached at axial strain equals to 40%). Specifically, for SS tests, the CSL is defined by extrapolating the experimental results for an extra 5% shear strain  $\gamma$ . As shown in Figure 5,  $\lambda_{cs} = 0.031$  and  $N_{cs} = 0.78$ .

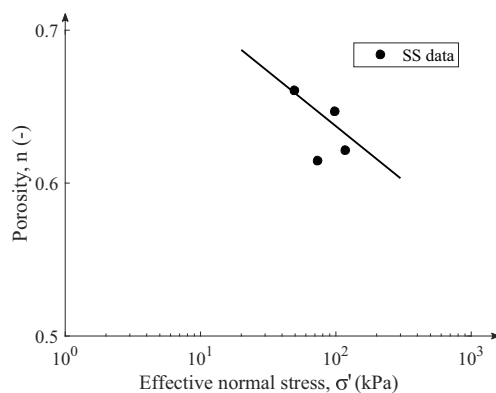
The model parameters characterising the dilatancy expression (Eq. 4) are calibrated based on simple shear tests on saturated and unsaturated specimens. The experimental values of dilatancy are computed as  $D = \Delta\varepsilon/\Delta\gamma$  by neglecting the elastic portion of the strain. As shown in Figure 6, a series of discrete values of the measured dilatancy is computed for every 0.4% increase in shear strain  $\gamma$  for a saturated sample (test ID. SSP0315) and an unsaturated sample (test ID. SSRPSG24). With a single set of dilatancy parameters being  $a_g = 0.001$ ,  $m_g = 0.99$ ,  $\mu_g = 0.2$ , and  $b = 0.02$  and considering the variation in  $\varphi$ , the pro-

**Table 1.** List of the test adopted to extrapolate shear strength envelope (data from [17], [16] and [18]).

Test type	Condition	Test ID.	$s$ [kPa]	$\sigma - u_a$ [kPa]	$\sigma'$
Simple Shear	sat	SSP0115	0.0	100.0	100.0
	sat	SSP0315	0.0	76.0	76.0
	sat	SSP0215	0.0	50.5	50.5
	unsat	SSRPSF03a	27.5	97.0	120.1
	unsat	SSRPSF03b	14.7	75.4	138.6
	unsat	SSRPSG23	25.0	50.0	73.0
unsat	SSRPSG24	25.0	100.0	118.9	
Ditect Shear	sat	TASNRS21	0.0	9.0	9.0
	sat	TASNRS22	0.0	20.0	20.0
	sat	TASNRS23	0.0	29.0	29.0
	sat	TASNRS25	0.0	39.0	39.0
	sat	TASNRS24	0.0	54.0	54.0
	sat	TASNRS26	0.0	59.0	59.0
	sat	TASNRS29	0.0	69.0	69.0
	sat	TASNRS28	0.0	79.0	79.0
	sat	TASNRS27	0.0	104.0	104.0
	sat	TASNRS31	0.0	133.0	133.0
	sat	TASNRS32	0.0	135.0	135.0
	unsat	TAL0608	25.0	73.4	73.4
	unsat	TAL0808	45.0	50.0	50.0
	unsat	TAL1008	60.0	89.3	89.3
Test type	Condition	Test ID.	$s$ [kPa]	$p - u_a$ [kPa]	$p'$
Triaxial	sat	BIS2206	0.0	100.0	100.0
	sat	BIS2306	0.0	100.0	100.0
	sat	BIS2406	0.0	100.0	100.0
	sat	BIS2606	0.0	50.0	50.0
	sat	BIS2706	0.0	200.0	200.0
	sat	BIS2806	0.0	30.0	30.0
	sat	BIS2906	0.0	30.0	30.0

**Table 2.** Summary of the fixed model parameters

Category	Symbols	Unit	Pyroclastic soil
Elasticity	$E_r$	kPa	8000
	$G_r$	kPa	1000
	$\sigma_r$	kPa	1.0
	$n_E$	-	0.5
	$n_G$	-	0.8
Plasticity	$\alpha_g$	-	0.001
	$m_g$	-	0.99
	$\mu_g$	-	0.2
	$b$	1/kPa	0.02
	$\lambda$	-	0.06
CSL	$N_{cs}$	-	0.78
	$\lambda_{cs}$	-	0.031



**Figure 5.** Critical State Line for Simple Shear tests. By fitting the experimental data, the CSL in  $\log \sigma' - n$  space is defined with  $\lambda_{cs} = 0.031$  and  $N_{cs} = 0.78$

of the experimental data and capture the transition from contraction to dilation in unsaturated samples.

The elastic response has been modelled through a pressure-dependent hypoelastic model and the related parameters are calibrated by using SS tests on saturated specimens. Parameters  $E_r$ ,  $n_E$  are evaluated in the  $\sigma' - \varepsilon$  plane while  $G_r$ ,  $n_G$  are evaluated in the  $\tau - \gamma$  plane.

Finally, the hardening parameter ( $\lambda$ ) has been determined through a trial-and-error procedure being 0.06.

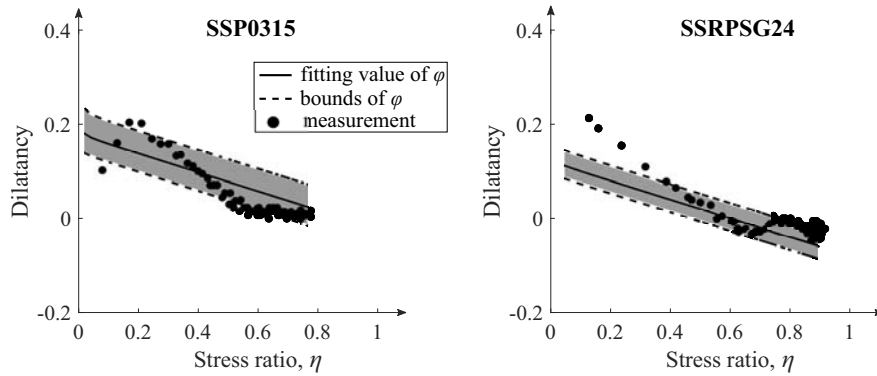
## 4 Role of the variability of pyroclastic soil properties

As discussed above, most of the parameters can be determined according to their physical meaning, as well as with the aid of the available experimental datasets. However, the estimation of some material properties like friction angle and SWRC shows uncertainties and further investigation is needed to clarify their influence on the material response. For this reason, variability analyses are carried out to investigate the effect of the model parameters associated with frictional strength and water retention on the model performance. The fitting relationship obtained in Figure 1 and 4 is adopted to define a range constraining the upper and lower boundaries of selected material characteristics.

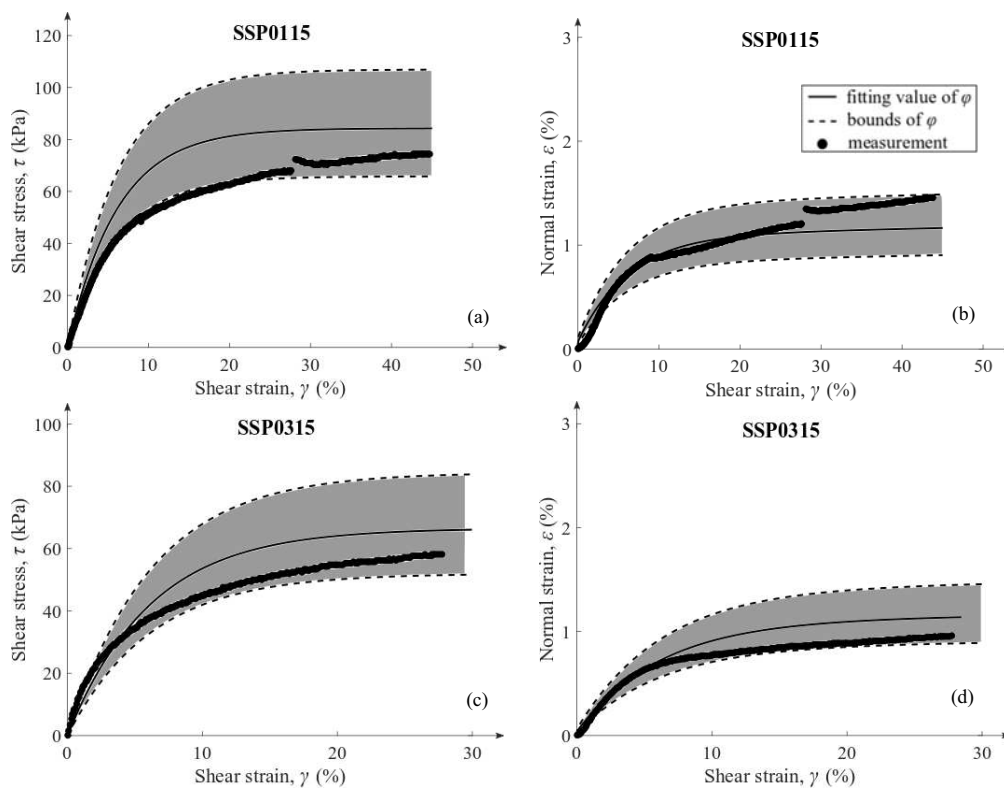
Figure 7 shows the model performance for two specific saturated samples (test ID. SSP0115 and SSP0315). The simulation results are represented by the shaded area formed by considering the variability in friction angle, furthermore in  $M_g$ , to reflect the uncertainty in shear strength envelope. The solid black curve represents the result from the curve fitting values, while the dashed boundaries imply the bounds associated with prediction bounds of  $\varphi$  of 95% confidence level. It is readily apparent that the experimental results are well captured by the prediction bounds for the considered samples.

Similarly, the analyses are repeated for two unsaturated samples (test ID. SSRPSG23 and SSRPSG24). And since the SWRC plays an important role in unsaturated samples, therefore, in addition to the variability of  $\varphi$ , also the variability of the constants governing the SWRC is considered. As presented in Figure 8, the predicted responses match satisfactorily the  $\gamma - \tau$  and  $\gamma - S_r$  relationship, but display mismatches in the  $\gamma - \varepsilon$  responses. However, the difference between measurements and predictions can be considered acceptable and the model is capable to properly replicate the experimental trend. Furthermore, it is worth to point out that unlike SSRPSG24, the change in the experimental results of  $S_r$  in sample SSRPSG23 is more severe, but it is included in the shaded area (Fig. 8c). The mismatch between experimental and numerical results can be due to the difference in the imposed loading rate upon shearing. The effect of loading rate needs to be further explored in future studies. In particular, future analyses may consider the possible emergence of suction heterogeneity in the proximity of instability conditions, which can in principle lead to transients reflecting a loss of equilibrium [19]. Similarly, further validation tests of the proposed calibration approach may involve the simulation of

proposed dilatancy law in Eq. 4 can reproduce the main trends



**Figure 6.** Calibration of dilatancy parameters with saturated and unsaturated samples: a) test ID. SSP0315; b) test ID. SSRPSG24. Model responses are obtained with  $a_g = 0.001$ ,  $m_g = 0.99$ ,  $\mu_g = 0.2$ , and  $b = 0.02$  considering the variability in friction angle  $\varphi$ .



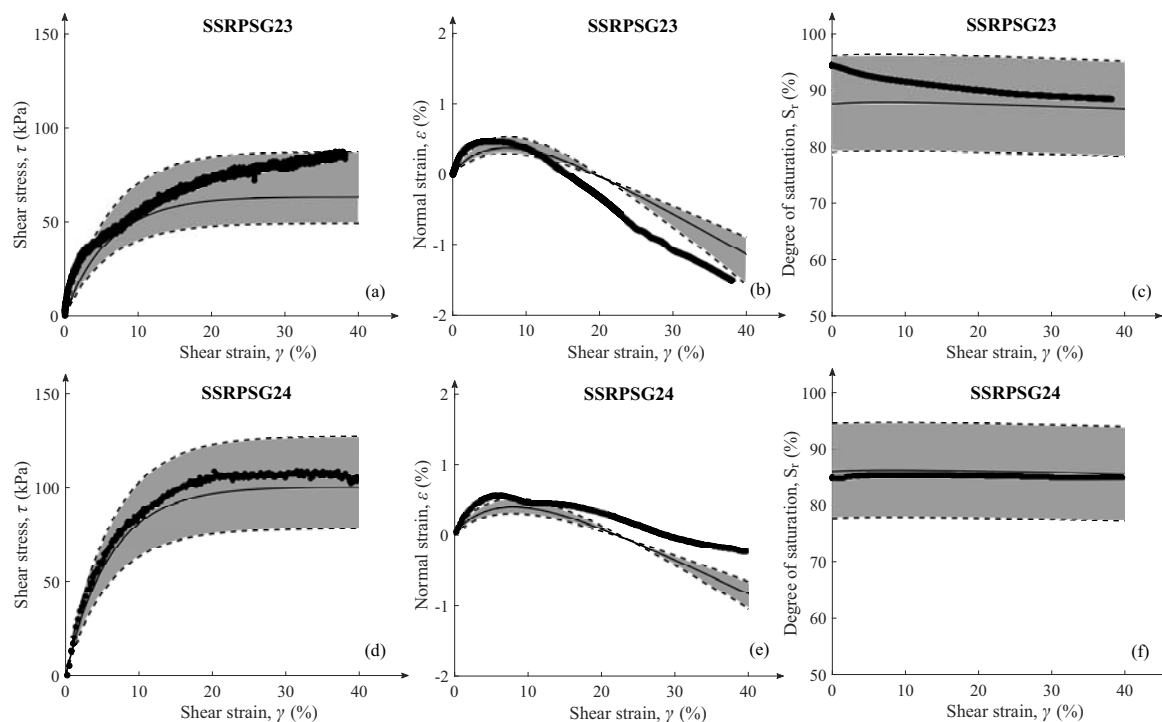
**Figure 7.** Simulations of SS tests under saturated conditions:(a)  $\gamma$ - $\tau$  response of test ID. SSP0115; (b)  $\gamma$ - $\varepsilon$  response of test ID. SSP0115; (c)  $\gamma$ - $\tau$  response of test ID. SSP0315; (d)  $\gamma$ - $\varepsilon$  response of test ID. SSP0315.

wetting tests, which are a known source of mechanical instabilities involving a flow-like behavior [20, 21].

## 5 Conclusion

The paper discusses the modelling of the simple shear tests performed on a volcanic soil sampled from Southern Italy. A constitutive model specialized for simple shear conditions has been proposed and multiple laboratory tests, including triaxial, direct and simple shear tests on saturated and unsaturated specimens, have been used to calibrate the model parameters, as well as to assess their range of variations in model and its effect on the material response. Specially, variability analyses were carried out to investigate

the impacts of changes in friction angle and SWRC properties. The model performance was evaluated by comparing the resulting simulations with data from simple shear tests conducted under constant suction and examined in  $\tau$ - $\gamma$  and  $\varepsilon$ - $\gamma$  and  $\gamma$ - $S_r$  planes. The results showed that, despite some inaccuracies in replicating the development of volumetric strains under unsaturated conditions, the model predictions agree satisfactorily with the available measurements. Most notably, the simulations illustrated that by constraining the model on the basis of the measured data scatter, it was possible to properly replicate the transition from a contractive to dilative behavior upon shearing observed for unsaturated samples. Future investigations will be required to better quantify the influence of suction on



**Figure 8.** Simulations of SS tests under unsaturated conditions:(a)  $\gamma$ - $\tau$  response of test ID. SSRPSG23; (b)  $\gamma$ - $\varepsilon$  response of test ID. SSRPSG23; (c)  $\gamma$ - $S_r$  response of test ID. SSRPSG23; (d)  $\gamma$ - $\tau$  response of test ID. SSRPSG24; (e)  $\gamma$ - $\varepsilon$  response of test ID. SSRPSG24 (f)  $\gamma$ - $S_r$  response of test ID. SSRPSG24.

the failure envelope and verify the model performance for wetting tests. Moreover, a further development may involve an explicit quantification of the agreement between data and computations based on automatic parameter optimization algorithms.

## Acknowledgements

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*Dear Editor, Dear Reviewer,*

*we are grateful for your useful suggestions. We carefully reviewed the comments and revised the manuscript accordingly.*

*Hereafter, in red color are the replies and/or the comments to your questions, as well as the description of the actions taken to tackle your queries.*

*Best regards,*

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Important dates:

FINAL REVISED PAPER: 31st December 2019

Contact: [info@eunsat2020.tecnico.ulisboa.pt](mailto:info@eunsat2020.tecnico.ulisboa.pt)

SUBMISSION: 42

TITLE: Modelling of simple shear tests on volcanic unsaturated sands

----- REVIEW 1 -----

SUBMISSION: 42

TITLE: Modelling of simple shear tests on volcanic unsaturated sands

AUTHORS: Mariagiovanna Moscariello, Yanni Chen, Sabatino Cuomo and Giuseppe Buscarnera

----- Overall evaluation -----

SCORE: 2 (minor revision)

----- TEXT:

The paper studies the response of simple shear tests on volcanic unsaturated sands in the context of a constitutive model for saturated and unsaturated conditions. An attempt to assess the influence of the experimental variability into the modelling is made with satisfactory results. I only have some minor comments and suggestions that may be considered by the authors.

Q1: On these latter aspects, I would perhaps suggest to the authors to specify that their work focuses on experimental variability with no attempts to model other sources of variability (e.g. spatial, model, etc.).

We agree with the reviewer that the paper is focused on assessing the role of experimental variability on the model performance. This paper aims to show the influence of the variation in soil properties on the model predictions, specifically, exploring the role of friction angle and SWRC parameters for simplicity purpose. However, more comprehensive investigations are suggested to explore the role of suction through the experimental data on wetting samples in the future. We have added some words in Section 4 of the manuscript to emphasize it.

Q2: One may wonder that the model parameters that have been estimated by ‘trial-and-error’ (i.e. hardening parameter  $\lambda$ ) or using fewer experimental data (e.g. critical states parameters) contain larger uncertainties than those estimated directly from available experiments. How (and how much) your results are affected by these uncertainties is not clear to me. It would be nice to see a small discussion on this aspect. Another aspect that I miss is how ‘model uncertainty’ influences the results presented in Figures 6-8 (see my last comment).

You are right, parameters determined through ‘trial-and-error’ could influence the simulations and they contain uncertainties which can’t be measured or estimated by the available experiments. Thus, they are considered as part of the sources of model uncertainty, but as our reply to your first comment, this work emphasizes the experimental uncertainties and explores the variations in soil properties on the model predictions. For this reason, we constrained our discussions on the effect of the variation in the admissible physical properties, specifically the frictional angle and SWRC, on the model performance while keeping the parameters reflecting model uncertainty constant to limit their influence. A brief discussion of this aspect can be found in the Introduction, as well as in Section 4.

Q3: The notation is a bit confusing. The symbol for effective stress  $\sigma'$  is used to refer to vertical direction only (see pg. 3 end of first column) normal effective stress (definition after Equation 3)? Does it refer to the mean effective stress?

Notation is clarified. The symbol  $\sigma'$  is used to refer to effective normal stress.

Q4: When using “ $n:\log\sigma'$ ” in pg 2 after Equation 5, what is the meaning of  $\sigma'$ ? Then strains components as defined, is  $\varepsilon$  referring to the normal strain which seems confusing if  $\sigma'$  relates to porosity (or if  $\sigma'$  the vertical effective stress as suggested in pg 3). My confusion on these aspects increases when looking at Table 1 (last column) because the variable included there is net stress. Please clarify and amend the text/figures accordingly.

$\sigma'$  is the effective normal stress, while  $n$  is porosity and  $\varepsilon$  is the normal strain. The CSL, here, is described in  $n-\log\sigma'$  plane, instead of more usual  $e-\log p'$ , where  $e$  is the void ratio and  $p'$  is the mean effective stress. In simple shear conditions, the mean effective stress is difficult to estimate without sophisticated simple shear equipment (i.e., the principal stresses cannot be determined directly). Only the normal and shear stresses on the horizontal boundaries are measured and it is not possible to construct the Mohr's circle stress. For this reason, the effective normal stress was considered more suitable than mean effective stress.

Table 1 was modified and the effective normal stress was added.

Q5: The equation appearing in Figure 4 should be presented as a proper equation in the text. It seems that the authors have taken this decision to fulfill the space restrictions. Perhaps table 1 can be summarised a bit to gain the necessary space to include the mentioned equation?

Figure 4 was modified and the equation was inserted in the text as eq. 9.

Q6: From the sentence “corresponding to zero suction” after Equation 5, one may think that full saturation is defined when suction is equal to zero (and not when degree of saturation is equal to 1). Is this the case? This matter should be clarified as it seems that saturated and unsaturated conditions have a marked different behaviour.

In terms of modelling, fully saturation is reached when suction being zero and it also indicates the degree of saturation is equal to 1. As suggested by the comment, we have modified the words after Equation 5 to clarify it.

Q7: The sentence: “However, due to the fact that suction is constant during shearing...” does this refer to the simulations? Figure 8b shows a quite substantial decrease of degree of saturation during the test (but not in the simulations). How do the authors explain this behaviour and why it is not captured by the model? This seems to suggest that the uncertainty on this aspect is, hence, due to model uncertainty rather than experimental variability in soil parameters investigated. Please comment.

Yes, the sentence refers to the simulation. During shearing, the suction is kept constant, but some change in the degree of saturation is observed and this is captured by the model through defining the water retention behaviour in terms of suction and volumetric water content. Thus, the model shows a slight change in the degree of saturation due to the change in the normal strain and it shows good match for Test ID SSRPSG 24. But as to Test ID SSRPSG 23, the experimental data shows a quite substantial change in the degree of saturation, while the simulation can't capture, which may be due to differences in the applied shear rate. Compared to SSRPSG24, SSRPSG 23 is carried out under a faster shear rate and it can be difficult for samples to reach suction equilibrium, and a further exploration is needed in the future study. This issue is briefly discussed in the third paragraph of Section 4 in the manuscript.