

Energy management of a dual-motor driven city bus based on reformed dynamic programming

Wenwei Wang¹, Hong Pan¹, Lin Cheng¹

¹National Engineering Laboratory for Electric Vehicles, Beijing Institute of Technology, Beijing, 100081, China

Abstract. This paper proposes a reformed dynamic programming (DP) based energy management strategy for a city bus driven by dual-motor coupling propulsion system(DMCPS). An instantaneous optimal problem of DMCPS's total energy loss is constructed to solve the torque allocation between two motors. Taking the results as extra constraints, a reformed DP architecture aimed at optimal energy consumption is established, where the state variables are the battery's SOC and operating modes of DMCPS, with a sole decision variable of mode switching action. The optimization results show a close performance to the original method, with the calculation efficiency greatly improved and the calculation time reduced by nearly 97%. To obtain practical rules for real-time application, the mode switching schedule is extracted based on a RBF-SVM classifier, and the torque allocation is ruled by linear function. Simulation results demonstrate that the extracted rules can be executed through an on-board processor, with energy consumption reduced by 2.19% compared to the original rule-based strategy.

1 Introduction

Dual-motor coupling propulsion system has great advantages in realizing the comprehensive performance of battery electric city bus, with great potential for energy saving [1]. And energy management strategy, which concludes torque allocation and mode switching, is one critical factor influencing its energy consumption. And due to its complex structure, a problem of balancing the strategy's optimum and practicability is proposed. Rule-based strategies have been widely utilized in practice with fast real-time calculation and good robust property [2-3]. However, it can hardly obtain the optimal energy consumption performance when it is only developed by empirical logic. On the contrary, optimization-based strategies based on dynamic programming can offer the global optimal policy, of which the real-time application is severely restricted by its large calculation workload [4-5]. Therefore, some researchers take offline global optimization results as reference to extract new control rules or recalibrate the original rules, which achieve a relative balance between both aspects [6-7].

In this paper, an energy management strategy for DMCPS based on reformed dynamic programming (DP) is proposed. In Section 2, the system configuration and operating modes are given and modeled. In Section 3, the reformed dynamic programming architecture is given,

based on the instantaneous optimal torque allocation for the system's total energy loss. The rule extraction method based on the optimization results is also introduced to solve the energy management problem in a typical driving cycle. The simulation results are illustrated, compared and discussed in Section 4 before conclusions are drawn in the final section.

2 Configuration, operating modes, and modelling of DMCPS

The dual-motor coupling propulsion system (DMCPS) studied in this paper is a centralized drive system, as shown in Fig.1. Here an auxiliary motor (EM2) equipped with a two-speed planetary transmission (AMT) and a traction motor (EM1) connected directly to the drive axle can drive the vehicle in a torque-coupling way. It is noted that the EM2 can be turned off and completely isolated from the EM1. Three different operating modes are defined for the system and distinguished by the gears of AMT, which includes gear 1 and gear 2 of dual-motor mode and gear 0 for EM1-only mode. Efficiency models of AMT and motors are constructed based on experiments by look-up table. Rint model is utilized for the battery. Power balance is established through vehicle dynamics.

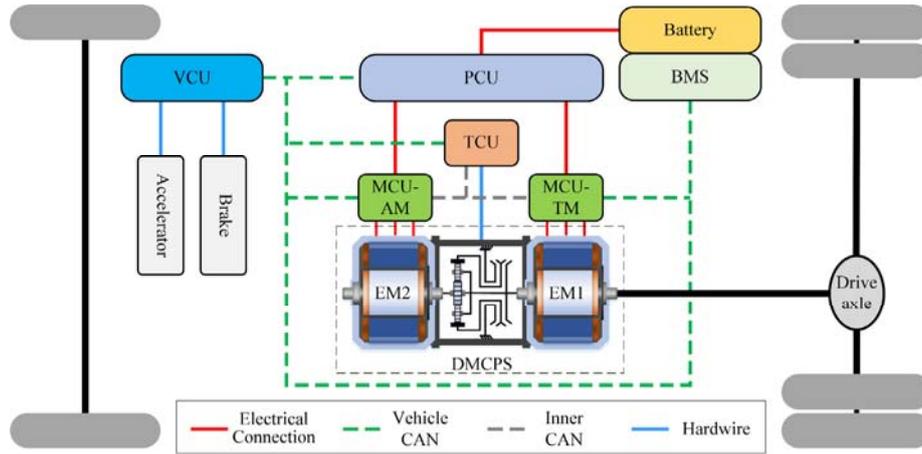


Fig.1 Configuration of the dual-motor coupling propulsion system

3 Energy management based on reformed DP

3.1 The torque allocation based on instantaneous optimal problem

The objective function of the instantaneous optimal problem is defined at a single sampling point instead of the entire working condition. If the current moment is k , then the objective function is the power the total power loss of the system. The problem can be expressed as:

$$[T_{EM1}^*(k), T_{EM2}^*(k)] = \underset{T_{EM1}(k) \in [T_{EM1,min}(k), T_{EM1,max}(k)]}{\operatorname{argmin}} \{P_{EM1,loss}(k) + P_{EM2,loss}(k) + P_{AMT,loss}(k)\} \quad (1)$$

where $T_{EMi}^*(k)$ is the optimal output torque and $P_{EMi,loss}(k)$ is the power loss of each motor EM_i , $i=1,2$. $P_{AMT,loss}(k)$ is the power loss on transmission. In order to improve the calculation efficiency, the power loss of

motor at a certain speed is fitted as a quadratic function of torque. Then the problem in Eq. (1) is equivalent to the following quadratic programming problem:

$$\begin{aligned} & \min f(T_{EM1}(k), T_{EM2}(k)) \\ & = \begin{pmatrix} T_{EM1}(k) \\ T_{EM2}(k) \end{pmatrix}^T \begin{pmatrix} a_{EM1}(k) & 0 \\ 0 & a_{EM2}(k) \end{pmatrix} \begin{pmatrix} T_{EM1}(k) \\ T_{EM2}(k) \end{pmatrix} \\ & + \begin{pmatrix} b_{EM1}(k) \\ b_{EM2}(k) + (1 - \eta_g(k))\omega_{EM2}(k) \end{pmatrix}^T \begin{pmatrix} T_{EM1}(k) \\ T_{EM2}(k) \end{pmatrix} \end{aligned} \quad \text{subject to} \quad \begin{aligned} & \begin{pmatrix} T_{EM1}(k) \\ T_{EM2}(k) \end{pmatrix} \geq \begin{pmatrix} T_{EM1,min}(k) \\ T_{EM2,min}(k) \end{pmatrix} \\ & \begin{pmatrix} T_{EM1}(k) \\ T_{EM2}(k) \end{pmatrix} \leq \begin{pmatrix} T_{EM1,max}(k) \\ T_{EM2,max}(k) \end{pmatrix} \\ & \begin{pmatrix} 1 \\ i_g(k)\eta_g(k) \end{pmatrix}^T \begin{pmatrix} T_{EM1}(k) \\ T_{EM2}(k) \end{pmatrix} = T_{dem}(k) \end{aligned} \quad (2)$$

where, at moment k , $a_{EMi}(k)$, $b_{EMi}(k)$ are the second-order and first-order coefficient of the power loss function of EM_i , $T_{dem}(k)$ is the total demand torque of the system, $i_g(k)$ is the ratio and $\eta_g(k)$ is the efficiency of the gear of AMT respectively.

coefficient λ is added in both scheme. So the expressions of reformed DP are as follows:

3.2 The reformed dynamic programming architecture

$$\begin{cases} x(k+1) = f(x(k), u(k)) \\ x(k) = [SOC(k), gear(k)] \\ u(k) = shift(k) \\ J = \sum_0^{N-1} [P_{bat,total}(x(k), u(k), k) + \lambda \operatorname{sgn}|shift(k)|] \end{cases} \quad (3)$$

The reformed DP based energy management strategy has the following similarities and differences compared with the original solution:

2) Considering the optimization process, for the original DP, both decision variables are optimized in a same step; Under the reformed framework, the operating mode is given at first, and then the optimal torque is determined by the instantaneous optimization during the backward solving process of DP, of which the flow chart is shown in Figure 2.

1) Considering key definitions, the original dynamic programming scheme contains 2 state variables (battery SOC, operating mode), 2 decision variables (mode switching command, torque allocation coefficient); The reformed scheme has the same 2 state variables, but only one decision variable which is the mode switching command. To avoid frequent mode switching, a penalty

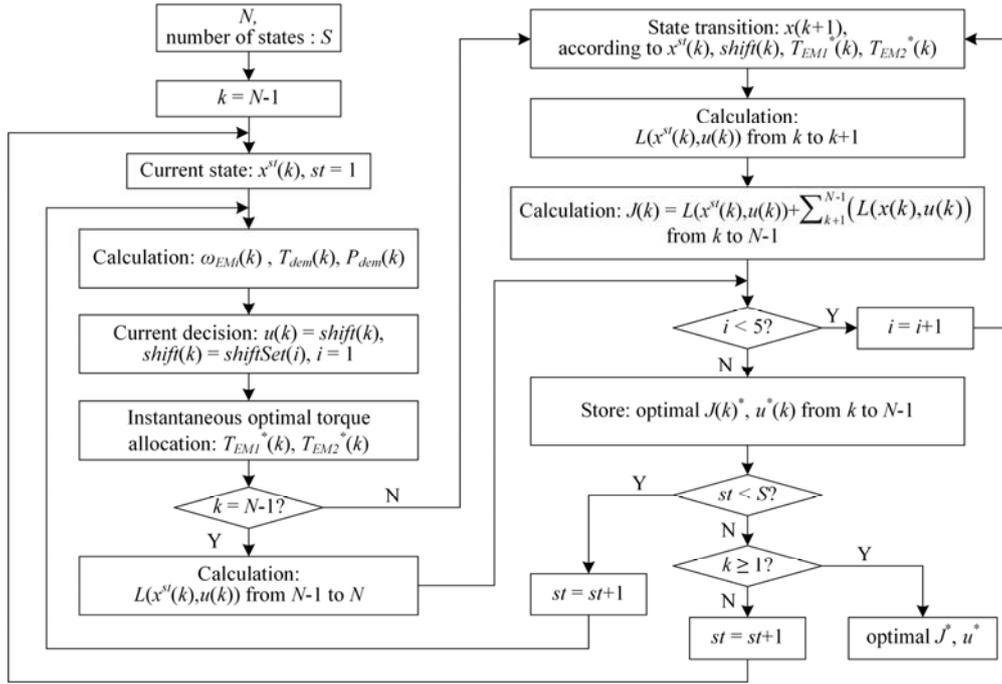


Fig.2 Backward solving process flow chart of reformed DP

3)The state and decision variables and λ of reformed DP are discretized by minor certain grids and resolution, as shown in table 1 with basic properties.

Table.1 Key variables of reformed DP

No.	Variables	Range	Resolution
1	State of charge (SOC)	0-1	0.004
2	Gear of the transmission (<i>gear</i>)	{0, 1, 2}	—
3	Mode Switching command (<i>shift</i>)	{-2, -1, 0, 1, 2}	—
4	Penalty coefficient (λ)	0 - $+\infty$	0.01

3.3 Optimization results and rules extraction

It is seen from the optimization results under C-WTVC shown in Fig.3 that the reformed DP has a pretty close energy consumption performance with the original DP,

which brings an increase of energy consumption by only 0.82%. In an environment with a processor of 2.30Ghz and RAM of 8GB, the solution time of the reformed DP is 14.620s, reduced by 97% compared to 413.556s of the original DP.

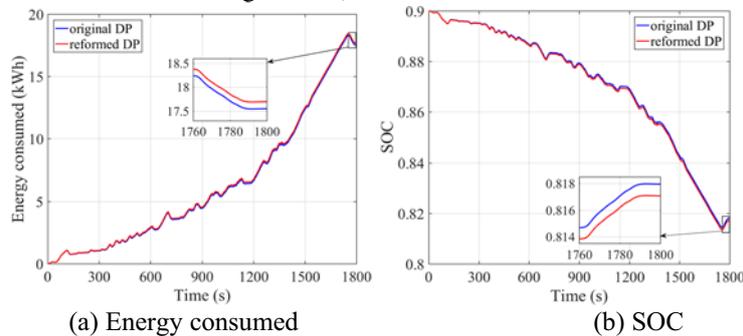


Fig.3 Energy consumption results of DP with 2 different architecture

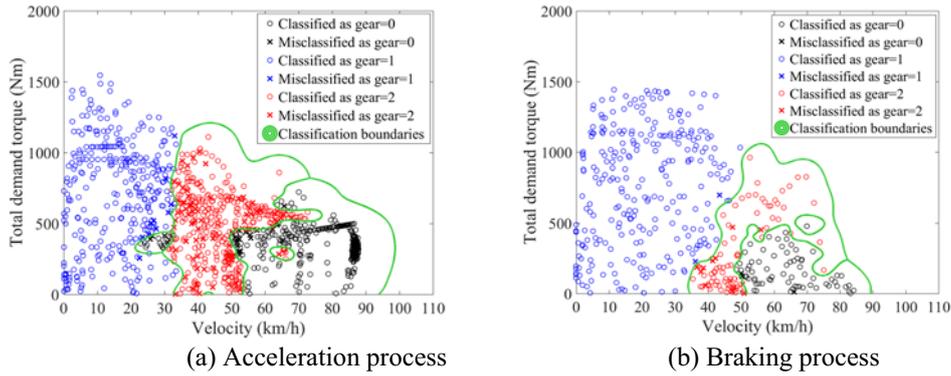


Fig.4 Classification results and boundaries of RBF-SVM classifier

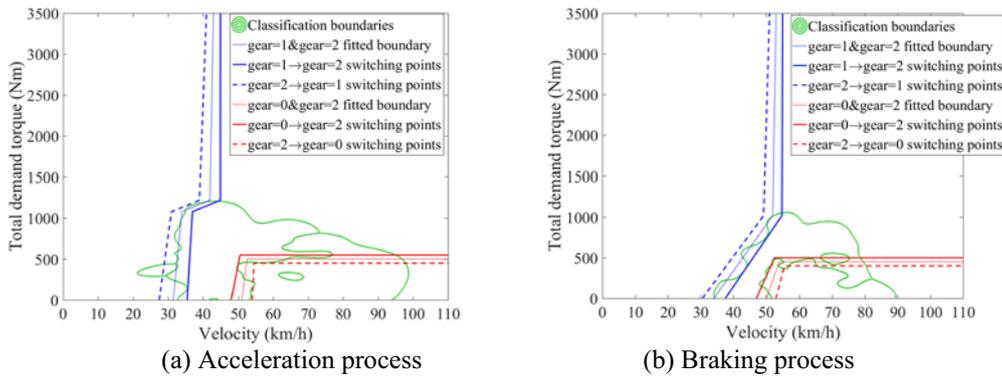


Fig.5 Mode switching rules based on classification boundaries

The mode switching rule is extracted based on a SVM classifier, of which the training set is the optimized operating modes distribution, the inputs are velocity and total demand torque, with a kernel function of radial basis function (RBF). The classification results and boundaries are shown in Fig.4. The results show that the accuracy of 10-fold cross-validation in driving and braking process is 90.0% and 94.9% respectively. Then the fitted boundaries and switching points can be formulated based on the classification boundaries, as shown in Fig.5, considering necessary delays in practical application.

And for torque allocation rules, to improve the efficiency of real-time application, the linear function between the optimal torque of EM1 and the total demand torque at a series reference speeds obtained by offline optimization is stored and used in practice through a look-up table.

The above extracted energy management rules applied to an electric city bus are simulated under C-WTVC in a hardware-in-the-loop platform with a designed controller unit.

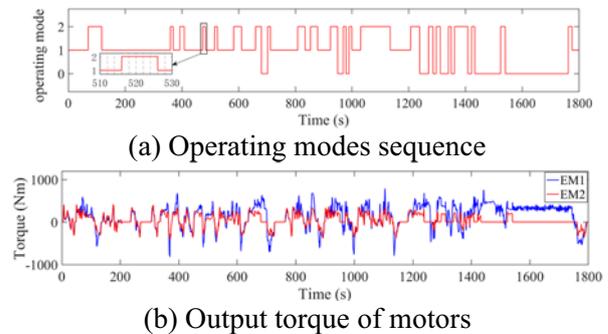


Fig.6 Operating modes and motor torque results of extracted rules

4 Simulation results and comparison

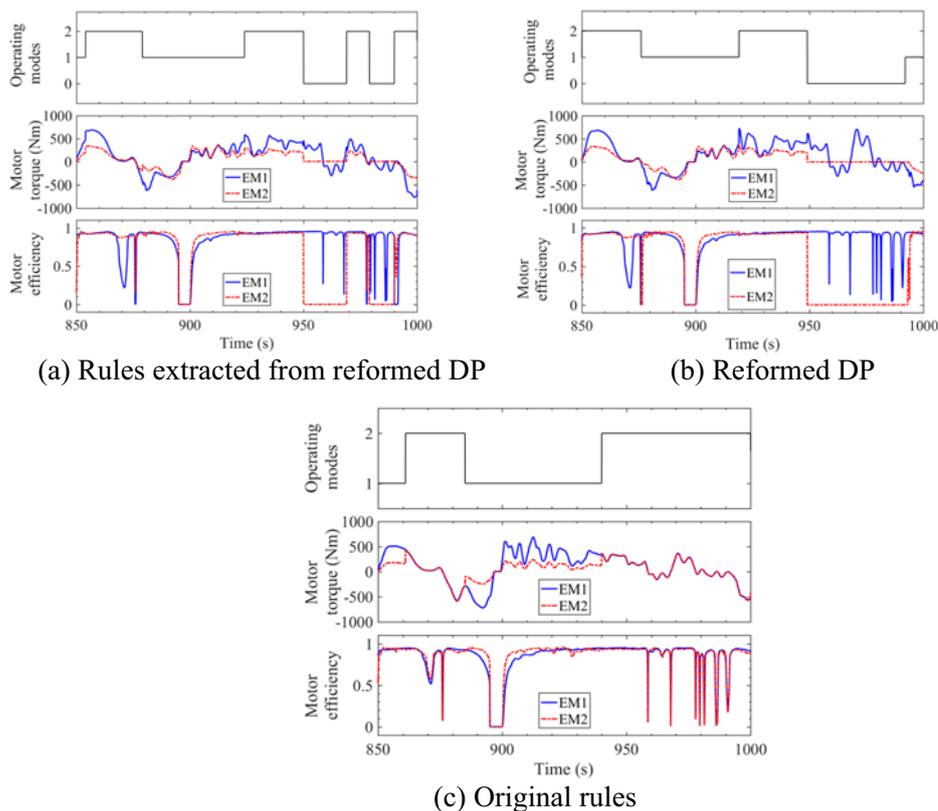


Fig.7 Results of a segment of the cycle of 3 different energy management strategies

It is seen from the results shown in Fig.6 that the operating mode under extracted rules has a reasonable switching frequency with a minimum interval of 10s, and the torque allocation results show a characteristic that the output of DMCPs is mainly provided by EM1 and supplemented by EM2. It is shown in Fig.7 that the extracted rules have a nearly same results, including the motors' efficiency, with the reformed DP, which indicates it can largely retain the control effect of the original strategy.

As is shown in Fig.8, the energy consumption per 100 kilometres of the extracted rules is 87.13kWh, only 0.72% higher than the reformed DP, and 2.19% lower than the original empirical rules, achieving an energy saving of 1.95kWh/100km; For the variation of SOC in a single cycle, the extraction rule is 0.0836, reduced by 0.0019 compared to the original rules.

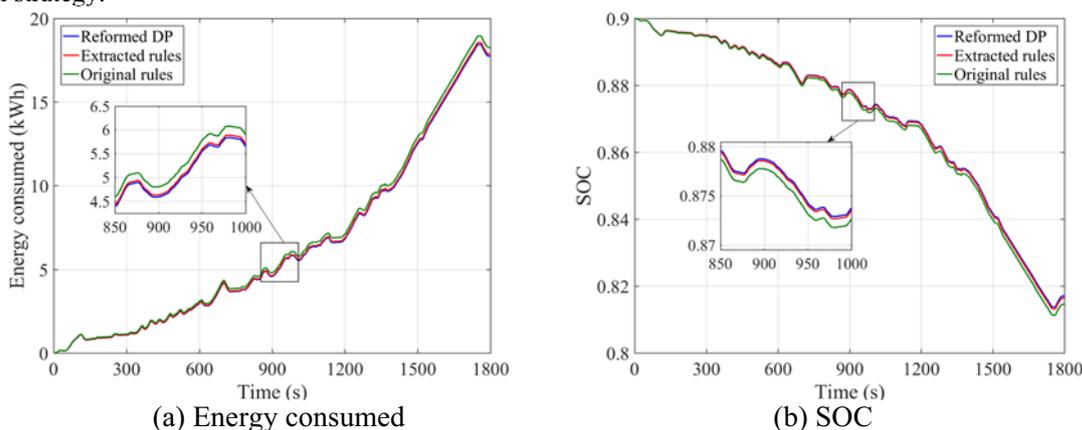


Fig.8 Energy consumption performance of 3 different energy management strategies

5 Conclusion

Based on the results and discussions presented above, the conclusions are obtained as below:

(1) It is shown that, for energy management of DMCPs-driven bus, the reformed DP has a rather close optimization effect with normal DP, with energy

consumption increasing by 0.82%, but achieves a significant reduction of calculation time of nearly 97%.

(2) The rules extracted from reformed DP through the proposed method is proven to be suitable and effective for real-time application in a battery city bus, realizing an energy consumption reduction by 2.19% compared to the original rule-based strategy.

Acknowledgments

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