

Ride comfort evaluation for a double-drum vibratory roller with semi-active hydraulic cab mount system

Nguyen Tien Duy¹, Le Van Quynh^{2}, Dang Viet Ha³, Bui Van Cuong² and Le Xuan Long²*

¹Faculty of Electronics Engineering, Thai Nguyen University of Technology, Thai Nguyen 24000, Vietnam

²Faculty of Automotive and Power Machinery Engineering, Thai Nguyen University of Technology, Thai Nguyen 24000, Vietnam

³Vietnam Register, Ha Noi 12059, Viet Nam

Abstract. The construction machinery market has required increasingly not only on working capacity but also ride comfort quality, therefore it has required increasing toward researchers and manufacturers. The main objective of this paper proposes and evaluates the performance of semi-active hydraulic cab mount system (SHCMs) of a double-drum vibratory roller in the direction of enhancing vehicle ride comfort under different operating conditions. Firstly, a nonlinear dynamic model of passive hydraulic cab mount system (PHCMs) is established to determine its vertical force which is connected with a dynamic model of vehicle - ground surface interaction. And then, a fuzzy logic controller (FLC) is designed to control the value of the damping force of SHCMs. Both the differential equations of motion and FLC are implemented in the MATLAB/Simulink environment. Finally, the ride performance of SHCMs is evaluated under different conditions according to ISO 2631: 1997 (E) standard. The obtained results show that the values of objective functions with SHCMs significantly reduce in comparison with PHCMs under different operating conditions.

1 Introduction

The earth-moving equipment often operate in harsh environments, sources of vibration are transmitted from the ground deformation, the internal combustion engine as well as the operating mechanism to the cab through cab mount system and driver's seat suspension system. Many research results have shown that driver works for a long time under vibration and shock environment, it can easily cause a series of occupational diseases such as spinal deformities, stomach diseases, etc. Especially, driver exposure for a long time with low frequency and large amplitude vibration which can cause physical discomfort or even diseases [1-2]. The topic of the ride comfort of earth-moving equipment is always of interest to researchers and manufacturers. The auxiliary cab mount system (ACMs) and main cab mount system (MCMs) of a vibratory roller were considered to solve the problem

*Corresponding author: lequynh@tnut.edu.vn

of cab shaking under low frequency excitation and then the design parameters of ACMs were optimized by the finite element method [3, 5]. An auxiliary damping mount (ADM) of a vibratory roller was proposed to control the cab shaking based on a half-vehicle dynamics model [4]. The design parameters of rubber cab mount system of a single-drum vibratory roller were optimized by GA (Genetic Algorithm) [6] and NSGA II (Non-dominated Sorting Genetic Algorithm II) [7]. The dynamic characteristics of the vibratory roller and mount cab system were analyzed by both simulation and experimental methods [8]. A hydraulic cab mount system (HCMs) of an earth-moving machinery was proposed and evaluated its ride performance in comparison with the rubber cab mount system using a 3-D dynamic model of the cab with six degrees of freedom(DOF) [9]. The hydraulic cab mount system (HCMs) of a drum vibratory roller was proposed to evaluate the ride performance in comparison with two types of the rubber cab mount system (RCMs) and pneumatic cab mount system (PCMs) using a 3-D nonlinear vehicle dynamics model with eleven degrees of freedom [10]. The hydro pneumatic cab mount system (HPCMs) of a vibratory roller was proposed investigate the ride effectiveness of HPCMs in the direction of enhancing vehicle ride comfort [11]. In order to enhance the off-road vehicle ride comfort, many control methods have been used to control the semi-active or active mount systems of earth-moving equipment. A combination of fuzzy logic controller and PID controller was applied to control the damping coefficient of semi-active cab mount system of vibratory roller using a nonlinear vehicle dynamic model [12]. A fuzzy logic controller (FLC) was designed to control the damping coefficient value of the semi-active hydro-pneumatic cab mount system of a vibratory roller [13]. Similarly, a fuzzy controller was designed to control a kind of magneto-rheological (MR) damper of a semi-active mount system of vibratory roller using a 2-DOF dynamic model [14]. An optimal fuzzy-PID control method was designed to control for a semi-active hydraulic cab mount system using a three-dimensional nonlinear dynamic model of vibratory roller[15].

The main idea of this paper is to propose a semi-active hydraulic cab mount system (SHCMs) for a double-drum vibratory roller based on the development of the structure of a passive hydraulic cab mount system (PHCMs) with adjustable hydraulic damping force of hydraulic actuator. Firstly, a nonlinear dynamic model of passive hydraulic cab mount system (PHCMs) is established to determine its vertical force which is connected with a dynamic model of vehicle - ground surface interaction. And then, a fuzzy logic controller (FLC) is designed to control the value of the damping force of SHCMs. Finally, the ride performance of SHCMs is evaluated through the root-mean-square (RMS) of acceleration responses (a_{ws} , m/s^2 and $a_{wcp\text{hi}}$, rad/s^2) based on ISO 2631: 1997 (E) standard [16] when vehicle operates under survey conditions.

2 Nonlinear dynamic model of hydraulic cab mount

2.1 Passive hydraulic cab mount (PHCM)

The structural diagram of a passive hydraulic cab mount (PHCM) with the orifices consists of rubber part, two oil chambers such as lower and upper chambers, and the fluid flowing up and down through the orifice derived from the damping plate driven by the bolt, the damping plate and the orifices, as shown in Fig.1(a). A nonlinear dynamics model is established based on the structural diagram of Fig.1(a) to determine its vertical force, as shown in Fig.1 (b), where, m_c and m_b are vehicle body mass and cab mass, respectively, p_1 and p_2 are the upper liquid chamber and the lower liquid chamber, respectively, z_c and z_b are the vertical displacements of cab and vehicle body masses, respectively, k_r and c_r are

stiffness and damping coefficients of rubber part, respectively and F_c is the total vertical forces of hydraulic cab mount.

Based on Fig. 1 (b), the total vertical forces of PHCM could be achieved by

$$F_{ch} = F_r + F_h \tag{1}$$

where, F_r is the vertical force of rubber part which is defined by Eq.(2) and F_h is the damping force of the hydraulic actuator with the orifices which is defined by Eq.(7).

$$F_r = k_r (z_c - z_b) + c_r (\dot{z}_c - \dot{z}_b) \tag{2}$$

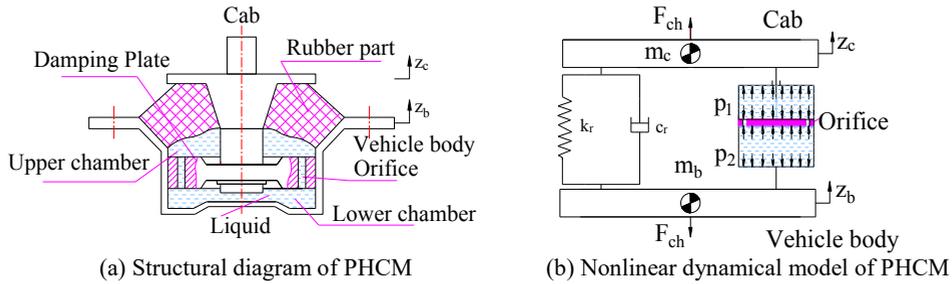


Fig. 1. Model of a passive hydraulic cab mount (PHCM) with the orifices.

The damping force of PHCM is determined by

$$F_h = \Delta p A_d \tag{3}$$

where, Δp is the pressure loss at the orifices, A_d is the effective area of the damping plate. Based on the reference [10, 17], the pressure loss at the orifices is determined by

$$\Delta p_0 = c_0 |\dot{z}_0| \dot{z}_0 \tag{4}$$

where, c_0 is the positive constant which is function of the geometry of the orifice and the fluid property, and \dot{z}_0 is the average flow velocities in the orifices

The equation of continuity for the flow through the orifice is written as follows

$$A_c \dot{z} = A_a \dot{z}_a \tag{5}$$

where, A_c and A_a are the effective area of the chamber and the orifices, respectively, \dot{z} is the relative velocity between the displacements of the vehicle body and cab masses.

Substitute Eq. (5) into Eq. (4), the pressure loss at the orifices can be achieved by

$$\Delta p_0 = c_0 \left(\frac{A_c}{A_a} \right)^2 |\dot{z}| \dot{z} \tag{6}$$

Substitute Eq. (6) into Eq. (4), the vertical damping force of the hydraulic actuator with the fluid flow through the orifices can be achieved by

$$F_h = c_0 A_d \left(\frac{A_c}{A_a} \right)^2 |\dot{z}| \dot{z} = c_f |\dot{z}| \dot{z} \tag{7}$$

2.2 Semi-active hydraulic cab mount (SHCM)

A control model for a semi-active hydraulic cab mount (SHCM) is developed from a model of passive hydraulic cab mount (PHCM) in Fig.1(b) with adjustable hydraulic damping force of hydraulic actuator, as shown in Fig.2, where, c_{semi} is the variable damping coefficient of hydraulic actuator of SHCM.

Based on Fig. 2, the total vertical forces of PHCM could be achieved by

$$F_{cs} = F_r + F_h + f \tag{8}$$

where, F_r is the vertical force of rubber part which is defined by Eq.(2), F_h is the damping force of the hydraulic actuator with the orifices which is defined by Eq.(7) and f is the adjustable damping force of the hydraulic actuator which is defined by fuzzy logic controller.

The controller design for a semi-active hydraulic cab mount (SHCM) of a double-drum vibratory roller will be presented below

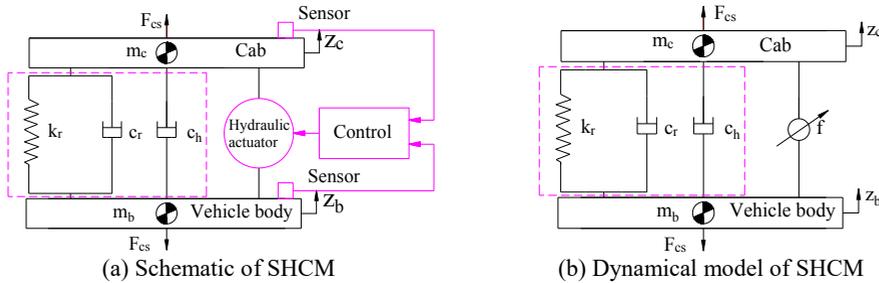


Fig. 2. Model of a semi-active hydraulic cab mount (SHCM).

Design of fuzzy logic controller (FLC): To adjust damping force of hydraulic actuator of the SHCM, a fuzzy logic controller is designed with two input variables such the relative displacement of SHCM, e and the relative velocity of SHCM c_e and an output control variable damping force of SHCM f . Seven triangular fuzzy sets for input/output variables including NB, NM, NS, ZE, PS, PM, PB in Table 1. The domain of variables are defined by $e \in [-0.4, 0.4]$ m, $c_e \in [-0.8, 0.8]$ m/s and $f \in [-2000, 2000]$ N. The values of the shape of membership functions are between 0 and 1. The control law system is designed as shown in Table 2.

Table 1. Language label symbols for fuzzy sets

NB	NM	NS	ZE	PS	PM	PB
Negative Big	Negative Medium	Negative Small	Zero	Positive Small	Positive Medium	Positive Big

Table 2. Rule base for fuzzy control

f		e						
		NB	NM	NS	ZE	PS	PM	PB
c _e	NB	PB	PB	PB	PB	PS	PM	PB
	NM	PB	PM	PM	PM	PM	ZE	NS
	NS	PB	PM	PM	PS	ZE	NS	NM
	ZE	PB	PM	PS	ZE	NS	NM	NM
	PS	PM	PS	ZE	NS	NM	NM	NB
	PM	PS	ZE	NB	NM	NB	NB	NB
	PS	ZE	NB	NM	NB	NB	NB	NB

3 Half-vehicle Dynamic Model

A structure diagram of a double-drum vibratory roller is selected for the ride performance evaluation of a semi-active hydraulic cab mount system (SHCMs) which consists of the mount and suspension systems such as the dynamic drum mount systems, the cab mount system and driver’s seat suspension system, as shown in Fig.3. A dynamic model of vehicle - ground surface interaction is developed from the structure of a double-drum vibratory roller in Fig.3, as shown in Fig.4 where, m_{di} , m_b , m_c and m_s are the masses of the dynamic drums, frame, cab and driver’s seat, respectively; I_b and I_c are the moment of inertia of m_b ,

and m_c , respectively; k_{sb} , k_{db} , k_s and c_{sb} , c_{db} , c_s are the stiffness and damping coefficients of elastic road surfaces, front and rear mount systems of drums and driver's seat suspension system, respectively; z_{db} , z_b , z_c and z_s are the vertical displacements of the front and rear drums, vehicle body, cab and driver's seat, respectively; φ_b and φ_c are the pitch angle displacements of vehicle body and cab, respectively; q_i are the front and rear drum absolute hard road excitations, respectively; l_j are the distances; $F_{ei}=F_{0i}\sin(\omega_i t)$ are the force excitations of the dynamic drums; F_{0i} are the amplitude of force excitations; ω_i are the angular frequencies of the vibrators; F_{ci} are the vertical forces of cab mount system and v is the vehicle speed ($i=1\div 2, j=1\div 6$).

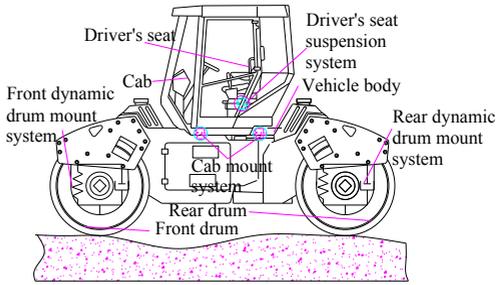


Fig. 3. Structure diagram of a double-drum vibratory roller

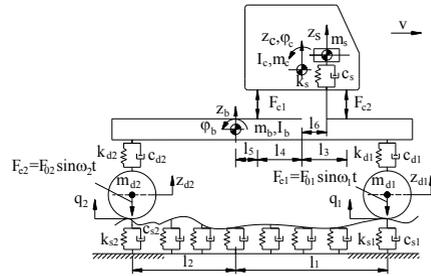


Fig. 4. A dynamic model of vehicle-ground surface interaction

The differential equation describing the vibrations in Fig.4. are written by a combined method of the multi-body system theory and D'Alembert's principle.

The vibration equation of the vertical driver's seat is written as follows

$$m_s \ddot{z}_s = k_s (z_s - z_c - l_6 \varphi_c) + c_s (\dot{z}_s - \dot{z}_c - l_6 \dot{\varphi}_c) \tag{9}$$

The vibration equations of the vertical and pitching cab are written as follows

$$m_c \ddot{z}_c = [k_s (z_s - z_c - l_6 \varphi_c) + c_s (\dot{z}_s - \dot{z}_c - l_6 \dot{\varphi}_c)] - \sum_{i=1}^{i=2} F_{ci} \tag{10}$$

$$I_c \ddot{\varphi}_c = [k_s (z_s - z_c - l_6 \varphi_c) + c_s (\dot{z}_s - \dot{z}_c - l_6 \dot{\varphi}_c)] l_6 + \sum_{i=1}^{i=2} (-1)^i F_{ci} l_{i+2} \tag{11}$$

where, F_{ci} is the total vertical forces of cab mount system which is is defined by Eq.(12).

$$F_{ci} = F_{ri} + F_{hi} + \begin{cases} 0 & \text{with PHCMs} \\ f_i & \text{with SHCMs} \end{cases} \tag{12}$$

The vibration equations of the vertical and pitching vehicle body are written as follows

$$m_b \ddot{z}_b = \sum_{i=1}^{i=2} F_{ci} - \sum_{i=1}^{i=2} F_{di} \tag{13}$$

$$I_b \ddot{\varphi}_b = \sum_{i=1}^{i=2} (-1)^i F_{di} l_i + F_{c2} l_5 + F_{c1} \sum_{j=3}^{j=5} l_j \tag{14}$$

where, F_{di} are the vertical forces of front and rear mount systems of dynamic drums which could be determined through two cases.

Case 1: Vehicle operates in the workshop

Condition 1: When both front and rear drums compact on the original place, the differential equations describing the vertical vibrations of dynamic drums are written as follows

$$m_{d1} \ddot{z}_{d1} = F_{e1} + F_{d1} - k_{s1} z_{d1} - c_{s1} \dot{z}_{d1} \tag{15}$$

$$m_{d2} \ddot{z}_{d2} = F_{e2} + F_{d2} - k_{s2} z_{d2} - c_{s2} \dot{z}_{d2} \tag{16}$$

Condition 2: When front or rear dynamic drum compact on the elastic soil grounds, and rear or front dynamic drum moves on the rigid ground surfaces, the differential equations

describing the vertical vibrations of front or rear dynamic drums is determined by Eq. (15) or Eq.(16) and the vertical force of rear or front dynamic drum mount system is determined by Eq.(18) or Eq.(17).

Case 2: Vehicle moves into the workshop

Vehicle moves on a variety of ground surfaces such as the absolute hard and deformed ground surfaces. The dynamic drums move on the absolute hard road surface. The vertical forces of front and rear mount systems of dynamic drums are defined as

$$F_{d1} = k_{d1}(z_b + l_1\phi_b - q_1) + c_d(\dot{z}_b + l_1\dot{\phi}_b - \dot{q}_1) \tag{17}$$

$$F_{d2} = k_{d2}(z_b - l_2\phi_b - q_2) + c_{d2}(\dot{z}_b - l_2\dot{\phi}_b - \dot{q}_2) \tag{18}$$

where, q_1 and q_2 are the front - rear drum absolute hard road excitations according to the International Standards Organization (ISO 8608) [23].

4 Results and Discussion

To solve the equations describing the vibrations in Fig.4 and design the fuzzy logic controller (FLC) for the ride performance evaluation of a semi-active hydraulic cab mount system (SHCMs) compared to the passive hydraulic cab mount system (PHCMs), Matlab /Simulink environment software is applied to simulate and control with a set of parameters of the vehicle, the PHCMs, the elastic soil ground and road surface roughness in the references [19, 20]. The comparison results of a_s (Time domain acceleration response of the vertical driver’s seat) and a_{cphi} (Time domain acceleration response of cab’s pitch angle) with SHCMs and PHCMs when the front drum compacts with the soil ground parameters as $k_{s1}=1.0 \times 10^7$ N/m, $c_{s1}=2.1 \times 10^5$ (N.s/m) and the excitation force as $F_{01}=0.128 \times 10^6$ N, $f_1=48$ Hz and rear drum moves the very poor ground surface (ISO class E) at $v=3.5$ km/h (Condition 2 of Case 1) are shown in Fig.5.

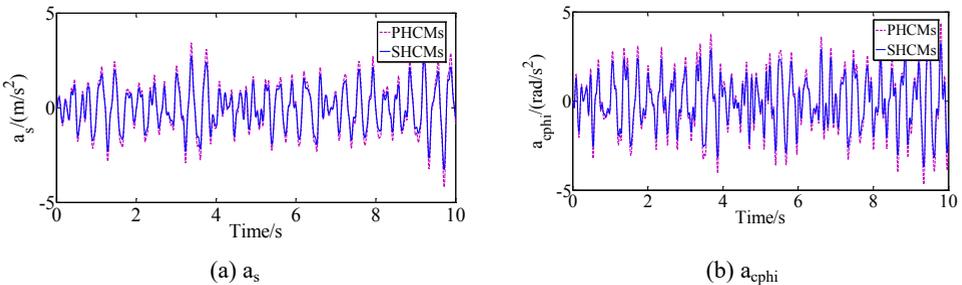


Fig. 5. The comparison results of a_s and a_{cphi} with SHCMs and PHCMs when the front drum compacts and rear drum moves under Condition 2 of Case 1.

The comparison results in Fig.5 show that the peak amplitude values of a_s and a_{cphi} with SHCMs respectively decrease compared to the PHCMs. Furthermore, we could be determined the values of a_{ws} and a_{wcphi} through Eq. (19) as $a_{ws} = 1.2865$ m/s², $a_{wcphi} = 1.6970$ rad/s² with PHCMs and $a_{ws} = 1.0305$ m/s², $a_{wcphi} = 1.3393$ rad/s² with SHCMs. The obtained results show that the a_{ws} and a_{wcphi} values with SHCMs respectively improve by 24.84% and 26.71% compared to PHCMs.

The values of a_{ws} and a_{wcphi} according to ISO standard 2631-1:1997 [16] are chosen as the objective functions which are defined by the formula below

$$a_{ws} = \left[\frac{1}{T} \int_0^T a_s^2(t) dt \right]^{\frac{1}{2}} \quad \text{and} \quad a_{wcphi} = \left[\frac{1}{T} \int_0^T a_{cphi}^2(t) dt \right]^{\frac{1}{2}} \tag{19}$$

where, T is the simulation time in s.

Similarly, the comparison results of a_s and a_{cphi} with SHCMs and PHCMs when vehicle moves on the poor ground surface (the ISO class D) at $v = 5$ km/h (Case2) are shown in Fig.6.

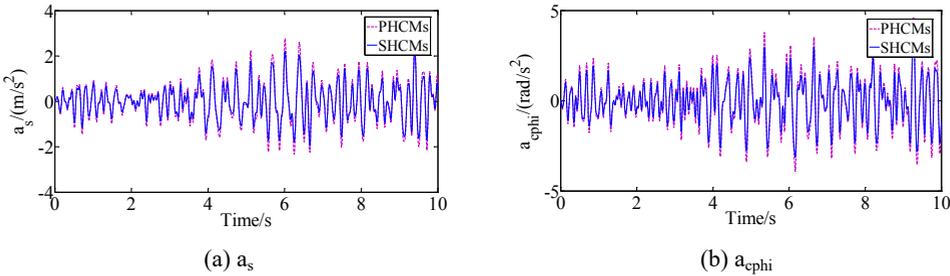


Fig. 6. The comparison results of a_s and a_{cphi} with SHCMs and PHCMs at Case 2

The comparison results in Fig.6 could be determined the values of the values of a_{ws} and a_{wphi} as $a_{ws} = 0.8982 \text{ m/s}^2$, $a_{wphi} = 1.3667 \text{ rad/s}^2$ with PHCMs and $a_{ws} = 0.7307 \text{ m/s}^2$, $a_{wphi} = 1.1111 \text{ rad/s}^2$ with SHCMs. The obtained results show that the a_{ws} and a_{wphi} values with SHCMs respectively improve by 22.92 % and 23.00% compared to PHCMs at Case 2.

The ride performance of SHCMs in comparison with PHCMs is verified and evaluated under several operating conditions.

Case 1 such as the both front and rear drums compact on the original place (Condition 1 of Case 1 with the soil ground parameters as $k_{s1} = 1.0 \times 10^7 \text{ N/m}$, $c_{s1} = 2.1 \times 10^5 \text{ N.s/m}$ and $k_{s2} = 1.2 \times 10^7 \text{ N/m}$, $c_{s2} = 2.8 \times 10^5 \text{ N.s/m}$ at the front and rear drum excitation forces as $F_{01} = 0.128 \times 10^6 \text{ N}$, $f_1 = 48 \text{ Hz}$ and $F_{02} = 0.96 \times 10^5 \text{ N}$, $f_2 = 54 \text{ Hz}$), the front drum compacts and rear drum moves the very poor ground surface (ISO class E) at $v = 3.5 \text{ km/h}$ (Condition 2 of Case 1), and the rear drum compacts and front drum moves the very poor ground surface at $v = 3.5 \text{ km/h}$ (Condition 3 of Case 1 with the soil ground parameters as $k_{s2} = 1.2 \times 10^7 \text{ N/m}$, $c_{s2} = 2.8 \times 10^5 \text{ N.s/m}$ at the rear drum excitation force as $F_{02} = 0.96 \times 10^5 \text{ N}$, $f_2 = 54 \text{ Hz}$). The values of a_{ws} and a_{wphi} at Conditions of Case 1 are shown in Fig.7. The comparison results show that the a_{ws} and a_{wphi} values with SHCMs respectively improved by 21.13% and 22.09% with Condition 1, 24.84 % and 26.71% with Condition 2 and 24.65% and 22.10% with Condition 3 in comparison with PHCMs.

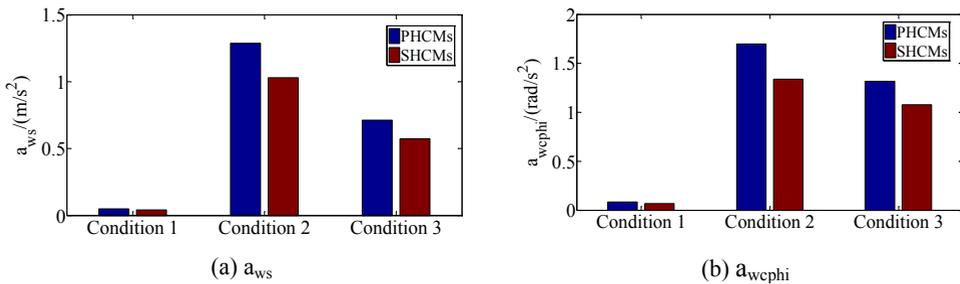


Fig. 7. The comparison results of a_{ws} and a_{wphi} with SHCMs and PHCMs at three different conditions of Case 1

Case 2, vehicle speed conditions of $v = [3 \ 5 \ 7 \ 9 \ 11] \text{ km/h}$ are selected for performance evaluation of SHCMs when vehicle moves on the poor ground surface (ISO class D). The values of the values of a_{ws} and (a_{wphi} at vehicle speed conditions of Case 2 are shown in Fig.8. The different ground surface conditions from the very good ground surface (ISO

class A) to very poor ground surface (ISO class E) are selected for performance evaluation at $v= 5 \text{ km/h}$. The values of a_{ws} and $a_{w\phi}$ at the ground surface conditions of Case 2 are shown in Fig.9.

The comparison results in Fig.8 show that the values of a_{ws} and $a_{w\phi}$ with SHCMs respectively improve by 22.28 % and 22.03 % with $v= 3 \text{ km/h}$, 22.92 % and 23.00 % with $v= 5 \text{ km/h}$, 23.35 % and 22.95 % with $v= 7 \text{ km/h}$, 27.11 % and 26.44 % with $v= 9 \text{ km/h}$ and 26.29 % and 26.23 % with $v=11 \text{ km/h}$ compared to PHCMs.

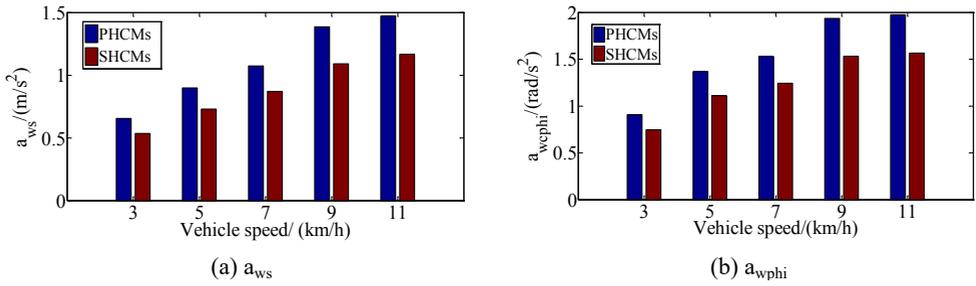


Fig. 8. The comparison results of the a_{ws} and $a_{w\phi}$ with SHCMs and PHCMs at five different vehicle speed conditions of Case 2

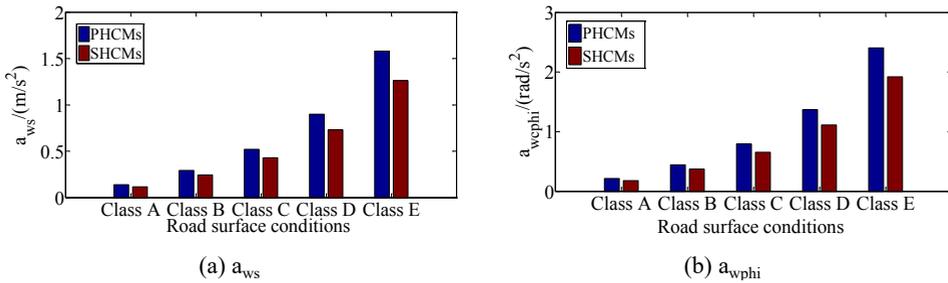


Fig. 9. The comparison results of a_{ws} and $a_{w\phi}$ with SHCMs and PHCMs at five different road surface conditions of Case 2

Similarly, the comparison results in Fig.9 show that the values of a_{ws} and $a_{w\phi}$ with SHCMs significantly decrease compared to PHCMs when ground surface conditions become bad. The results reflect that vehicle ride comfort with SHCMs is better than the PHCMs results as indicated by a_{ws} and $a_{w\phi}$ values. Thus, the ride performance of SHCMs with FLC has significantly improved vehicle ride comfort compared to PHCMs under low excitation frequencies and large amplitudes of road surface.

5 Conclusions

In this paper, a semi-active hydraulic cab mount system (SHCMs) of a double-drum vibratory roller was proposed on the basis of the development of the structure of a passive hydraulic cab mount system (PHCMs) with adjustable damping force of hydraulic actuator. The FLC was used to control damping force of SHCMs. The ride performance of SHCMs was evaluated based on a dynamic model of vehicle - ground surface interaction under survey conditions and ISO 2631-1(1997). The main study conclusions drawn from the comparative evaluation results are: (1) The values of a_{ws} and $a_{w\phi}$ with SHCMs respectively improve by 22.92 % and 23.00% in comparison with PHCMs at Condition 2 of

Case 1 and the ride performance of SHCMs has significantly reduced vibrations compared to PHCMs at Condition 2 of Case1; (2) the values of a_{ws} and $a_{w\phi}$ with SHCMs respectively improve by 22.92 % and 23.00% compared to PHCMs at Case 2 and (3) The ride performance of SHCMs has significantly improved vehicle ride comfort compared to PHCMs under the survey conditions. In addition, the obtained results give a useful material for researchers and manufacturers in the field of suspension system and mount system design for earth-moving machinery.

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