

Maximum Power Extraction of Solar PV system using DC-DC Buck converter and backstepping control based on P&O MPPT algorithm

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Abstract. This paper presents the system allowing the extraction of maximum power from a sun based on solar photovoltaic module and backstepping control based on a P&O MPPT algorithm for a DC-DC buck converter. The aim of this research work is to determinate quickly the optimal PV Module working point which allowed to extract the maximum power. This work, based on a usage of a DC-DC buck converter to control the working point by adjusting PV voltage through a duty cycle. In order to achieve our goal, we used the combination of perturb and observe (P&O) algorithm and DC-DC buck converter with backstepping control. This model was implemented in Matlab/Simulink software, the results of simulation prove its effectiveness in term of maximum power tracking dynamics for different irradiance and temperature profiles.

1 Introduction

Since the industrial revolution, the energy mix of most countries across the world has become dominated by fossil fuels [2]. This has major implications for the global climate, as well as for human health. This is why the whole world is moving towards low-carbon sources and renewable energy.

At our national level, Morocco also has adopted this strategy of ecological modernization with an ambitious program aimed at increasing the share of renewable energies (for electricity needs) in the national energy network to 42 % by 2021, 52 % by 2030 and 100% by 2050 (Fig1) [4], by launching megaprojects in areas related to solar and wind energy [5-6-7].

These energies: photovoltaic energy and wind energy present several challenges because of its intermittent and variable nature during the day and from one season to another, this why scientific researchers try through their researchers to make the use and conversion of these energies more efficient, profitable, competitive and therefore more interesting. The primary concern of the researchers is to increase the efficiency of the PV energy conversion operation by implementing high performance MPPT algorithms and the design of efficient energy converter structures. There are about twenty methods for tracking the Maximum Power Point (MPPT), whose efficiency and speed vary [8]. The most commonly encountered methods are:

- Perturb and Observe (P&O) [9-15]
- The IncCond (Incremental conductance) [15]
- The Fractional Open-circuit Voltage method (FOC)
- The Fractional Short-circuit Current method (FSC)

In this research, we choose to use the P&O MPPT algorithm for designing our MPPT control based on

Buck structure for DC-DC CONVERSION. In order to achieve a good control performance in term of dynamics and precision, we used the backstepping technique for the control design of the DC-DC buck converter. In the first, we present the PV Module model and its behaviour for variation of radiation and temperature, in the third section we present the DC-DC Buck converter model, then in the fourth section, we present the DC-DC Buck converter control design using backstepping technique, after that in the fifth section, we present our MPPT algorithm based on the principal of Perturb and Observe (P&O), finally sixth section we give the simulation results of the PV conversion control, followed by conclusion [1].

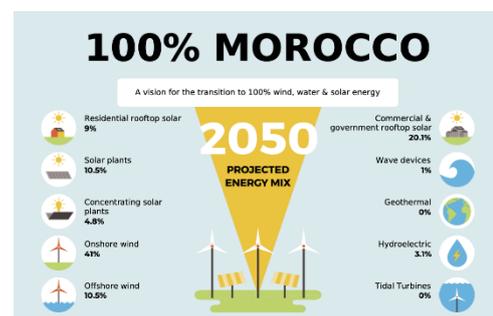


Fig.1. The vision of renewable energy with 100% by 2050 [5]

2 Model of photovoltaic module

A photovoltaic PV generator is the whole assembly of solar cells, connections, protective parts, supports, etc. In the present modeling, the focus is only on cell/module/array. Solar cells consist of a PN junction fabricated in a thin wafer or layer of semiconductor (usually silicon) [16]. In the dark, the I-V output characteristic of a solar cell has an exponential

characteristic similar to that of a diode. When solar energy (photons) hits the solar cell, with energy greater than the band gap energy of the semiconductor, electrons are knocked loose from the atoms in the material, creating electron-hole pairs. These carriers are swept apart under the influence of the internal electric fields of the PN junction and create a current proportional to the incident radiation [16]. When the cell is short circuited, this current flows in the external circuit; when open circuited, this current is shunted internally by the intrinsic PN junction diode. The characteristics of this diode therefore set the open circuit voltage characteristics of the cell [16].

2.1 Modelling the solar cell

In this research, we use the single diode equivalent circuit model as shown in Fig.2, to simulate PV Module voltage-current (V-I) behavior [1]. The main model parameters comprise the photogenerated current (I_{ph}), saturation current (I_{ss}), diode ideality factor (η). Series resistance (R_s) and shunt resistance (R_p). These parameter values are given in Table 1.

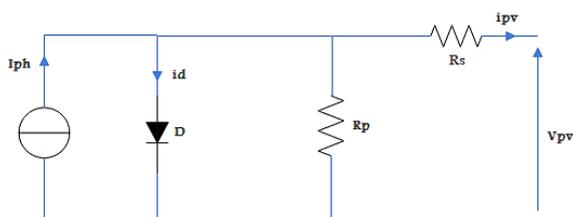


Fig. 2. The equivalent circuit of a PV cell

The photovoltaic module can be modeled mathematically as given in equations:

- Saturation current:

$$I_{ss} = I_{rs} \cdot \left(\frac{T}{T_n}\right)^3 \cdot \exp\left[\frac{q \cdot E_g \cdot \left(\frac{1}{T_n} - \frac{1}{T}\right)}{\eta \cdot K}\right] \quad (1)$$

- Photo-current:

$$I_{ph} = [I_{sc} + k_i \cdot (T - 298)] \cdot \frac{G}{1000} \quad (2)$$

- Reverse saturation current:

$$I_{rs} = \frac{I_{sc}}{\exp\left[\frac{q \cdot V_{oc}}{\eta \cdot N_s \cdot K \cdot T}\right] - 1} \quad (3)$$

- Shunt current:

$$I_{sh} = \left(\frac{V_{pv} + R_s \cdot i_{pv}}{R_p}\right) \quad (4)$$

In this model the output current can be expressed as follows:

$$I_{pv} = I_{ph} - I_{ss} * \left(\exp\left(\frac{q \cdot (V_{pv} + R_s \cdot i_{pv})}{\eta \cdot K \cdot T \cdot N_s}\right) - 1\right) - I_{sh} \quad (5)$$

Where:

q: is the elementary charge ($q=1,602 \cdot 10^{-19} \text{ e}$)

K: is the Boltzmann constant ($K=1,38 \cdot 10^{-23} \text{ J.K}^{-1}$)

G: is the irradiance (W/m^2)

T: is the temperature (K)

T_n: is the temperature for standard test conditions

I_{sc}: is the short circuit current (A)

V_{oc}: is the open circuit voltage (V)

N_s: number of cells connected in series

N_p: number of PV modules connected in parallel

E_g: Band gap energy of the semiconductor (1,1 eV)

The photogenerated current i_{ph} and open circuit voltage V_{oc} can be calculated from rated parameter's value of the PV module, as follows:

Table 1. The PV module parameters

Parameters		Values	Units
P	Nominal power	60	W
V _{oc}	Open circuit voltage	21,1	V
I _{sc}	Short circuit current	3,8	A
k _i	Current temperature coefficients	0,0025	mA/K
k _v	Voltage temperature coefficients	-0,08	V/K
R _s	Series resistance	0,18	Ω
R _p	Parallel resistance	360	Ω
η	Ideality factor of the diode	1,36	-

2.2 Influence of temperature and irradiance

In order to illustrate the PV model behavior, we present below in Figure 3 to Figure 6, the current-voltage and power-voltage curves of the model in case of various temperature value with constant irradiation as shown in Figure 3 and Figure 4, and in case of various value of irradiation with constant temperature value as shown in Figure 5 and Figure 6.

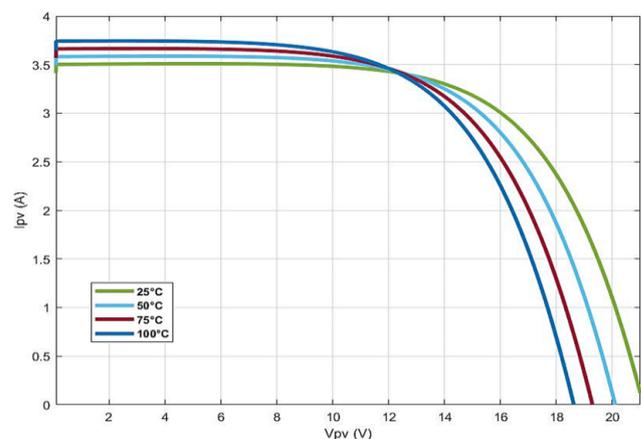


Fig.3. I_{pv} - V_{pv} PV Module curves for irradiance $E=1000 \text{ W/m}^2$, and for different temperature values

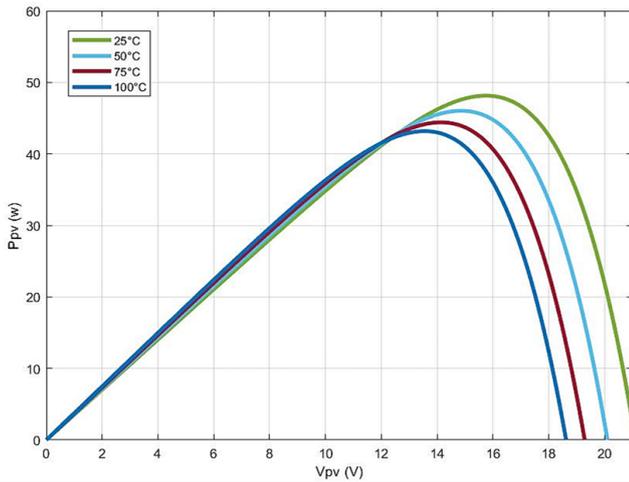


Fig.4. Ppv-Vpv PV Module curves for irradiance E=1000 W/m², and for different temperature values

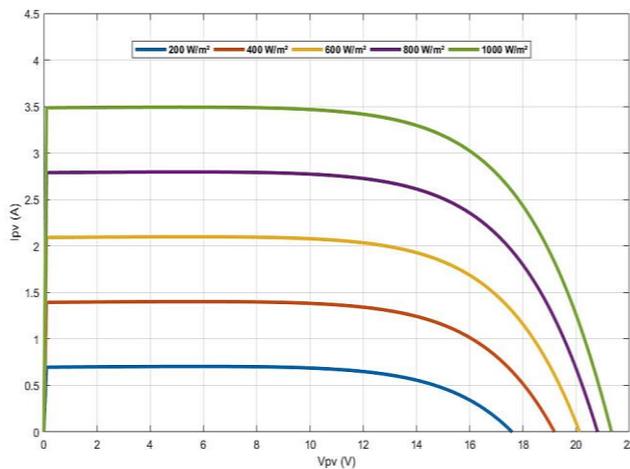


Fig.5. Ipv-Vpv PV Module curves for temperature T = 25°C, and for different irradiance values

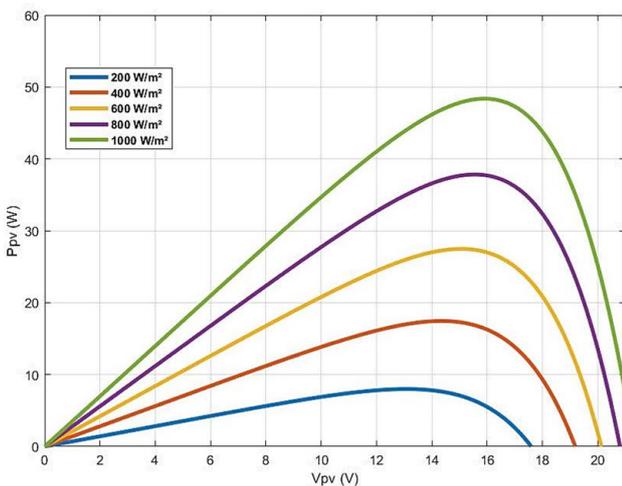


Fig.6. Ipv-Vpv PV Module curves for temperature T = 25°C, and for different irradiance values

3 Buck converter design

A buck converter (step-down converter) is a DC-DC power converter which steps down voltage (while stepping up current) from its input (supply) to its output (load). It is class of switched-mode power supply, typically containing at least two semiconductors (a

diode and a transistor) and at least one energy storage voltage ripple, filters made of capacitors are normally added to the converter output (load-side filter) and input (supply-side filter) [12].

In this work, we choose to use a DC-DC buck converter as showing in Fig.7 to achieve load adaptation in order to make PC Module work at its maximum power point. We consider this converter is more adequate for PV-MPPT control, because it allows us to control the input voltage V_e , which is equal to the PC Module voltage V_{pv} .

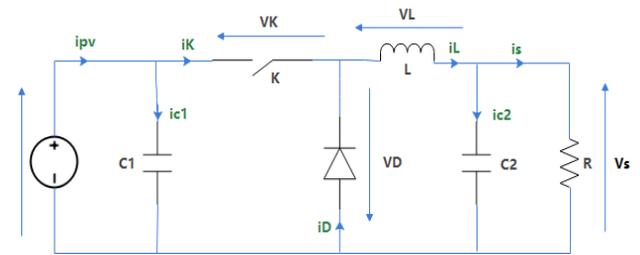


Fig.7. Buck converter circuit

The parameters values used are given in this table below:

Table 2. The Buck converter parameters

Parameters	Values	Units
C1	Input capacitor	1000 μ F
C2	Output capacitor	1000 μ F
L	Input inductance	100 mH

The switch component K is commuted periodically as described below:

- K On and D Off, for $(0 \leq t \leq dT)$:

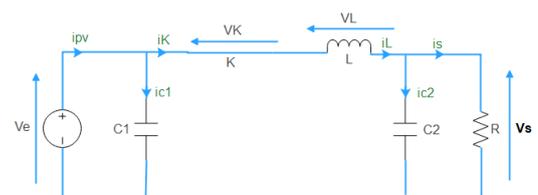


Fig.8. Buck converter for $(0 \leq t \leq dT)$

In this phase the current in the inductance is given by the following equation:

$$\frac{di_L}{dt} = \frac{v_e - v_s}{L} \quad (6)$$

The I_{pv} current is given by the following equation:

$$\frac{dv_e}{dt} = \frac{i_L - i_{pv}}{C1} \quad (7)$$

The output voltage V_s is given by the following equation:

$$\frac{dv_s}{dt} = \frac{i_L - i_s}{C2} \quad (8)$$

- K Off and D On, for ($dT \leq t \leq T$):

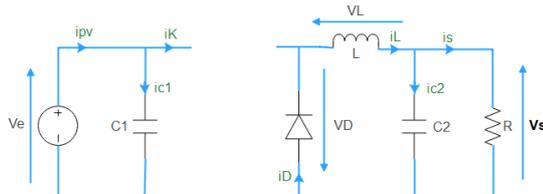


Fig.9. Buck converter for ($dT \leq t \leq T$)

In this phase we present the equation of the input voltage:

$$\frac{dVe}{dt} = -\frac{ipv}{C1} \quad (9)$$

The current variation in the inductance is given by following equation:

$$\frac{diL}{dt} = \frac{-vs}{L} \quad (10)$$

The output voltage Vs is given by the following equation:

$$\frac{dVs}{dt} = \frac{iL - is}{C2} \quad (11)$$

Based on these equations the Buck converter averaging model is as below:

$$\begin{cases} \frac{diL}{dt} = \frac{ve}{L} d - \frac{vs}{L} \\ \frac{dVe}{dt} = \frac{iL}{C1} d - \frac{ipv}{C1} \\ \frac{dVs}{dt} = \frac{iL - is}{C2} \end{cases} \quad (12)$$

4 Buck converter backstepping control

In this section we will give the study that allows determining the control law of the Buck converter offering desired performances. This control will help us to achieve the main goal, which is the extraction of maximum photovoltaic power, this control will be designed in two successive steps, and through a virtual variable command [1]. This control will be used to adjust output PV voltage in order to perform maximum power tracking.

4.1 First step: input variable control

In this step we design the control that ensures the good output voltage. So, we define below the first tracking error:

$$e_1 = V_s - V_{sref} \quad (13)$$

The error dynamic is given by:

$$\dot{e}_1 = \dot{V}_s - \dot{V}_{sref} \quad (14)$$

Based on the equation (12) we can express the error dynamic as below:

$$\dot{e}_1 = \frac{iL - is}{C2} - \dot{V}_{sref} \quad (15)$$

To ensure the first step control stability, we choose the Lyapunov Candidate Function (LCF) as following:

$$V_1 = \frac{1}{2} e_1^2 \quad (16)$$

The LCF dynamic is given as below:

$$\dot{V}_1 = e_1 \cdot \dot{e}_1 \quad (17)$$

$$\dot{V}_1 = e_1 \cdot \left(\frac{iL - is}{C2} - \dot{V}_{sref} \right) \quad (18)$$

In order to have $\dot{V}_1 < 0$, we supposed that:

$$\dot{e}_1 = -k_1 e_1 \quad (19)$$

Where k_1 is a positive constant

Based on (17) and (19), we can conclude this:

$$\dot{V}_1 = -k_1 e_1^2 < 0 \quad (20)$$

From (15) and (19), we obtain the following equation:

$$\frac{iL}{C2} - \frac{is}{C2} - \dot{V}_{sref} = -k_1 e_1 \quad (21)$$

We consider the following virtual variable command α , ensuring first step stability:

$$\alpha = \frac{iL}{C2} \quad (22)$$

In order to have a stable tracking error dynamic, we impose the following reference control of the virtual variable:

$$\alpha_{ref} = -k_1 e_1 + \frac{is}{C2} + \dot{V}_{sref} \quad (23)$$

4.2 Second step: virtual variable control

In this step we try to stabilize the tracking error of the following virtual command:

$$e_2 = \alpha - \alpha_{ref} \quad (24)$$

After derivation, we have the following dynamic equations of virtual control error e_2 :

$$\dot{e}_2 = \dot{\alpha} - \dot{\alpha}_{ref} \quad (25)$$

From (12) and (22), we can express the virtual control error as below:

$$\dot{e}_2 = \frac{1}{C2} \left(\frac{ve}{L} d - \frac{vs}{L} \right) - \dot{\alpha}_{rf} \quad (26)$$

The second LCF of global control is:

$$V_2 = \frac{1}{2} e_1^2 + \frac{1}{2} e_2^2 \quad (27)$$

After derivation we obtain:

$$\dot{V}_2 = e_1 e_2 - k1 e_1^2 + e_2 \cdot \dot{e}_2 \quad (28)$$

In order to have $\dot{V}_2 < 0$, we supposed that:

$$-k_2 e_2^2 = e_1 e_2 + e_2 \cdot \dot{e}_2 \quad (29)$$

Where k_2 is a positive constant.

So, we have to impose this following control law:

$$\dot{e}_2 = -k_2 e_2 - e_1 \quad (30)$$

From (26) and (30), we determinate the expression of control that ensure the stabilization of the buck converter control.

$$d = \frac{LC2}{Ve} \left[-k_2 e_2 - e_1 + \frac{Vs}{LC2} + \dot{\alpha}_{ref} \right] \quad (31)$$

5 Maximum Power Point Tracking algorithm

To improve the efficiency of the solar panel we use MPPT, in the present work we chose to use Perturb and Observe (P&O) algorithm [6].

The perturb and observe (P&O) algorithm is generally the most commonly applied in the control of MPPT of the PV generator. It had simple structure, low cost, easy to implement, reduced number of parameters, the possibility to introduce improvements and may result in top-level efficiency [9].

This algorithm (Fig.11) is depending on investigating the relation between PV module output power and its voltage. The behavior of solar panel indicating MPP and operating principle is shown in (Fig.10) which indicates that the resulting change of PV power is observed as follows:

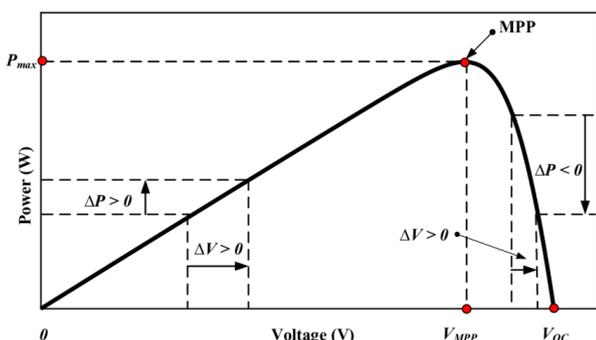


Fig.10. Characteristic curves of P&O MPPT technique [15]

If the PV module operating point is on the left side of the curve ($\Delta P_n / \Delta V_n$ is positive), which means the PV module output power increases, the perturbation of the PV module voltage should also be increased toward the MPP.

$\Delta P_n > 0$:

- $\Delta V_n > 0$: Should increased
- $\Delta V_n < 0$: Should decreased

If the operating point of the module was on the right side of the curve ($\Delta P_n / \Delta V_n$ is negative), then the perturbation of the PV module voltage should be decreased toward the MPP.

$\Delta P_n < 0$:

- $\Delta V_n < 0$: Should increased
- $\Delta V_n > 0$: Should decreased

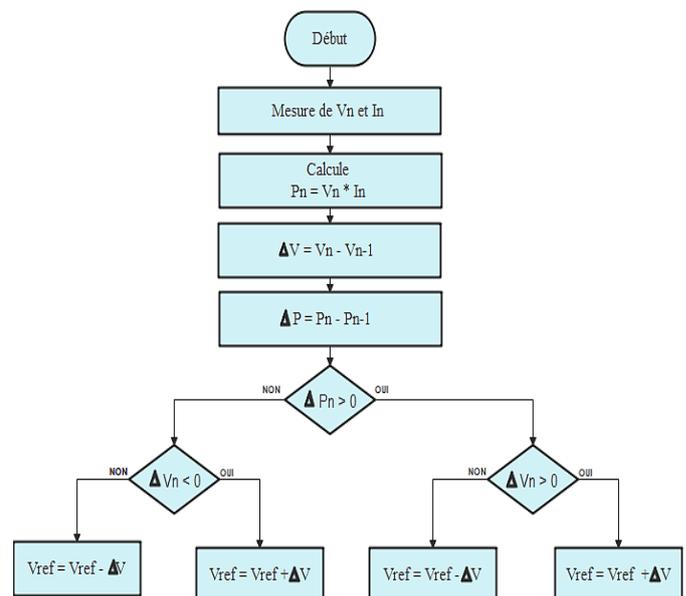


Fig.11. Flow Chart of P&O MPPT

For better performance and in order to have a precise and fast MPP tracking, we must correctly choose the step of V_{ref} increasing and decreasing. In this work we take a constant step equal to 0.001.

6 Simulation Results: Matlab/Simulink

In this section we present the validation of our PV conversion control, whose structure is given in Fig.12. In order to verify the effectiveness of the adopted solution, we have performed a set of simulation tests. The control validation is made, in first with different values of irradiance which are respectively in following intervals: [100, 600, 200, 400 W/m²], and in the second with different temperature which are [60, 25, 10, 40°C].

The determination of DC-DC converter load R_{load} is made by considering the steady state of the converter. When can establish following equation that represent R_{load} in function of duty (d):

$$R_{load} = d^2 \frac{I_{mpp}}{V_{mpp}} \quad \text{Where: } 0 < d < 1$$

So, we have to choose the resistance load while respecting this:

$$R < \frac{I_{mpp}}{V_{mpp}}$$

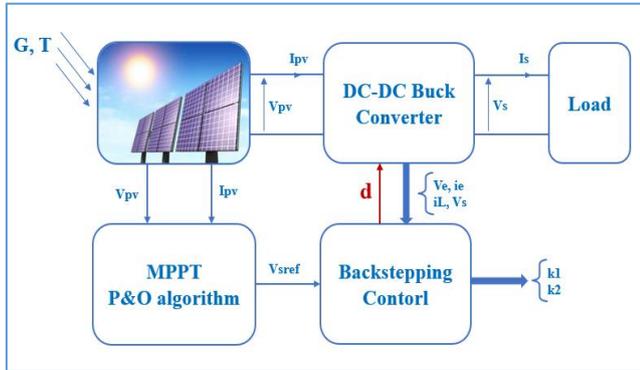


Fig.12. Structure of the MPPT- Backstepping control

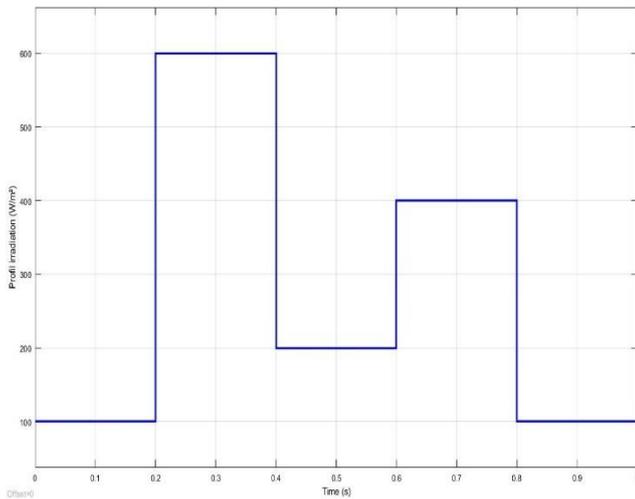


Fig.13. Profile irradiance

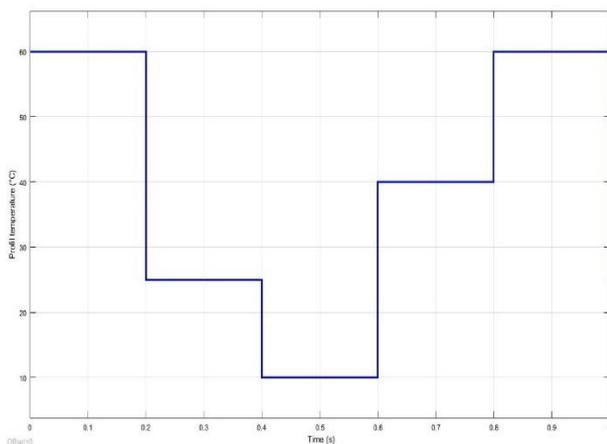


Fig.14. Profile temperature

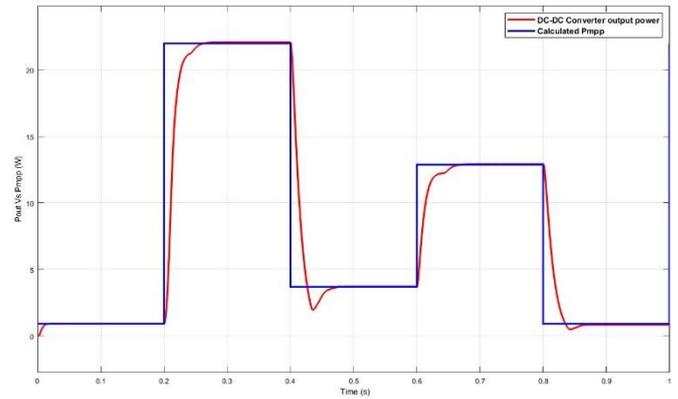


Fig.15. DC-DC Converter output power and calculated Pmpp

Fig.16 and Fig.17 shows that PV voltage track correctly the reference voltage.

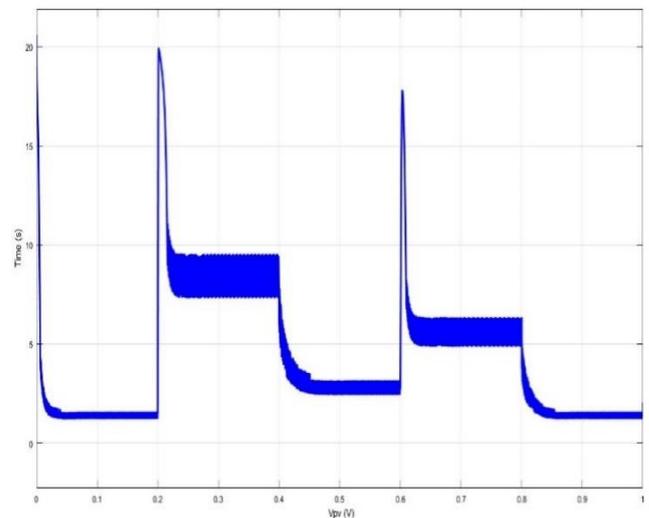


Fig.16. PV Voltage

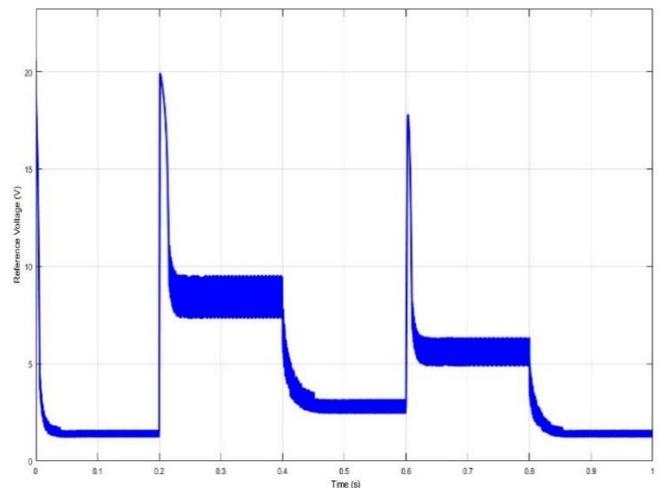


Fig. 17. Reference voltage

We can see in Fig.15 that the control ensures a fast and precise tracking of the maximum power of PV Module comparison with the MPP power.

Fig.18, Fig.19, and Fig.20 present respectively the inductance current, the output current and output voltage.

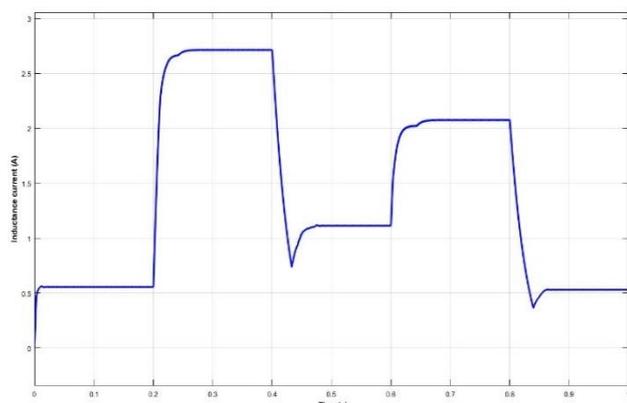


Fig.18. Inductance current

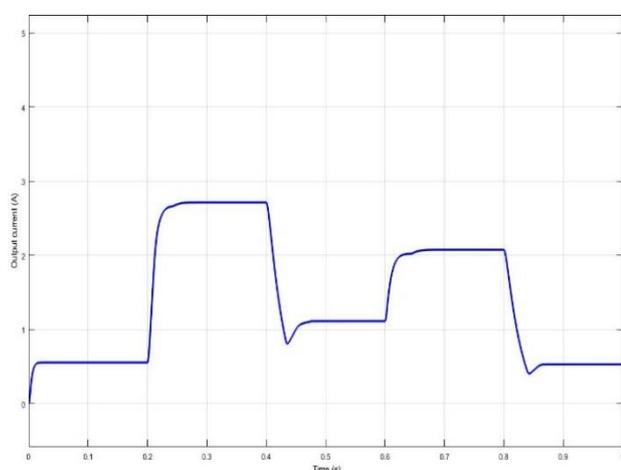


Fig.19. Output current

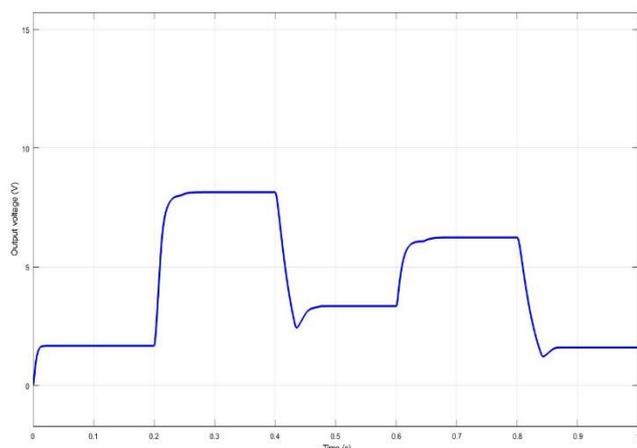


Fig.20. Output Voltage (Vs)

Conclusion

This article brings to light the steps taken to model the photovoltaic module from equivalent circuit and the equations of a solar cell. The photovoltaic module which is modeled with Simulink is then coupled the P&O

MPPT system, Backstepping control, and the DC-DC Converter.

In this paper, we developed a control based, in first part, on MPPT Algorithm using Perturb and Observe (P&O) technique, improved by reducing calculation time, by taking in consideration voltage and current ripples and by correctly choosing Voltage reference increasing step, and in second part, on Backstepping technique to control DC-DC Buck Converter, that provide good output voltage tracking to its voltage reference given by the MPPT Algorithm. As we have shown through simulations, this command gave good results in terms of stability, tracking quality, accuracy, and dynamic speed. The validation through simulation is done assuming hard profile of atmospheric conditions variation, more than it is in real conditions (with a large variation of temperature and irradiance, and it is made all this simulation conditions and results proof the effectiveness of our solution of conversion and MPPT control of photovoltaic energy.

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