

# Optimized Fractional Order Based Droop Control with Improving the Flexibility of a Microgrid

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**Abstract.** This work presents an improved four-levels hierarchical control strategy for flexible microgrid based on three-phase voltage source inverters (VSIs) connected in parallel. In the proposed strategy, zero-level control is required to handle current and voltage control of VSIs. The primary-level that consists of a decentralized controller is based on a modified universal droop control by introducing a fractional-order derivative. It is used to enhance the power sharing quality during islanded mode and the desired power generation in grid-connected mode. In the secondary centralized control, the voltage and frequency deviations caused by the primary-control are restored. Also, this level includes the synchronization control loop that enables a seamless transition between both operation modes. In order to improve the flexibility of the microgrid, a sequential logic approach is proposed in the tertiary level. It is exploited to manage both the restoration and the synchronization loops at each transition, as well as the static switch (SS) which is used to connect/disconnect the microgrid to/from the main grid. The control parameters are optimized by using the self-learning particle swarm optimizer (SLPSO) algorithm. Simulations were performed to highlight the performances of the proposed hierarchical control approach compared with the well-known three-levels control scheme.

## 1 Introduction

In recent years, the world has witnessed high levels of atmospheric pollution through large emissions of toxic gases that is a consequence of the high demand primarily for electric power [1], which gave an incentive to exploit renewable energy sources (RES)s such as wind energy, photovoltaic, tidal energy, thermal energy, etc, as clean and inexhaustible power sources to enhance energy security of countries and reduce imports of fossil fuels that are polluting the environment [2]. The RESs has gone through many stages of technological development in order to use them as an alternative to traditional energy sources in modern power grids and to facilitate support for the electrification of isolated

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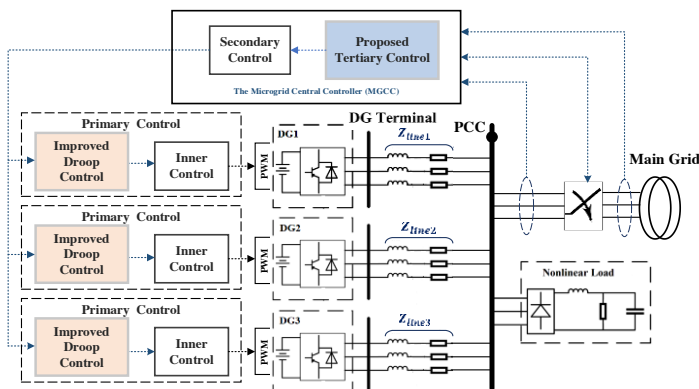
rural communities as well as affordability. The use of RESs also allows a transition from centralized production (the traditional model) to decentralized energy production.

The microgrid presents a privileged approach for the integration of decentralized energy resources. It combines multiple local production and distribution installations composed of distributed generation (DG) units, storage systems and loads. The considered DGs integrated with the AC microgrids are based on VSIs connected with passive harmonic filters to produce a scheduled voltage with a synchronous frequency. They are connected in parallel to the same bus with a local linear or nonlinear load. The microgrid can operate autonomously by handling power quality issues as well as interact with the main grid or with other microgrids, thus creating a Smart Grid. The microgrid is connected with the main grid via SS.

In this context, a new robust controller called the universal droop control is developed in [3], for an accurate power sharing regardless of the output impedance of the VSIs when the microgrid operates in islanded mode. Recent research is directed to design a hierarchical control for flexible operation of a microgrid [4]. The structure of this control strategy consists of three levels; inner, primary and secondary. The inner control is based on a cascade proportional resonant controller to get a better voltage and current regulation with less harmonics. A developed droop control is proposed as a primary controller. It makes the universal droop control able to handle the grid-connected mode. The secondary controller is required to restore the amplitude and frequency deviations caused by the primary controller. Also, it synchronizes the microgrid voltage with the main grid voltage for a smooth transition. Both the restoration loop and the synchronization loop and SS are not methodically managed at each transition.

In this work, a fractional order derivative is introduced to the universal droop control proposed in [4]. A tertiary level control, based on a sequential logic approach, is added to increase the flexibility of the microgrid. This level allows the secondary controller loops to operate autonomously, as well as the SS. The dynamic performances of the developed four levels hierarchical control are highlighted via simulations using MATLAB/SIMULINK, for a microgrid with three VSIs connected in parallel and a local nonlinear load.

The remainder of this paper is organized as follows: Section 2 presents the overall structure of the proposed four levels hierarchical control scheme. The improved primary control level with fractional order derivative including the inner controller is described. The PI centralized controller of the secondary level is presented. A sequential logical management strategy is developed for the tertiary control level. Optimized control parameters via SLPSO algorithm are given in section 3. Section 4 illustrates comparative simulation results with the well-known three levels control scheme. Section 5 concludes the paper.



**Fig. 1.** Block diagram of the microgrid including proposed hierarchical control scheme.



$D_t^{\mu_i}$  is the non-integer  $\mu_i^{th}$  order derivation operator  $\left(\frac{d}{dt}\right)^{\mu_i}$  with  $\{\mu_{1,2} \in \mathcal{R}^+ / 0 < \mu_1, \mu_2 < 2\}$ . Therefore, Laplace representation of the fractional-order operator is presented according to Grünwald-Letnikov in [5] as follow:

$$L\left(k_{fdP} D_t^{\mu_1}(P(t) - P^*)\right) = k_{fdP} s^{\mu_1}(P(s) - P^*) \quad (4)$$

$$L\left(k_{fdQ} D_t^{\mu_2}(Q(t) - Q^*)\right) = k_{fdQ} s^{\mu_2}(Q(s) - Q^*) \quad (5)$$

The method proposed by Oustaloup in [6] is based on the fractional order approximation by a function of a recursive filter called the Oustaloup filter. Considering  $[\omega_b, \omega_h]$  as the frequency band, The Oustaloup recursive approximation of  $s^{\mu_i}$  operator shown in Fig.2 is expressed by the following transfer function:

$$\hat{G}(s) = K \cdot \prod_{k=-N}^N \frac{(s + \omega'_k)}{(s + \omega_k)} \quad (6)$$

Where:

$$\begin{aligned} K &= \omega_h^{\mu_i} \\ \omega'_k &= \omega_b \left(\frac{\omega_h}{\omega_b}\right)^{\left(\frac{k+N+0.5(1-\mu_i)}{2N+1}\right)} \\ \omega_k &= \omega_b \left(\frac{\omega_h}{\omega_b}\right)^{\left(\frac{k+N+0.5(1+\mu_i)}{2N+1}\right)} \end{aligned} \quad (7)$$

$(2N + 1)$  is the filter order.

P and Q in Fig.2 are the active and the reactive power delivered by the power inverter. They are calculated from  $v_{pcc}$  and  $i_o$  through the following expression [7]:

$$p = v_{pcc\alpha} i_{o\alpha} + v_{pcc\beta} i_{o\beta} \quad (8)$$

$$q = v_{pcc\beta} i_{o\alpha} - v_{pcc\alpha} i_{o\beta} \quad (9)$$

$p$  and  $q$  are the instantaneous active and reactive power,  $v_{pcc\alpha\beta}$  and  $i_{o\alpha\beta}$  are the PCC voltage and the output current given by using the  $\alpha\beta$  transformation. Low pass filters are applied to obtain P and Q (Power Calculator Block).

The signal generated by the droop control through power sharing is considered as a reference signal  $v_{cref}$  of the capacitor voltage controller.

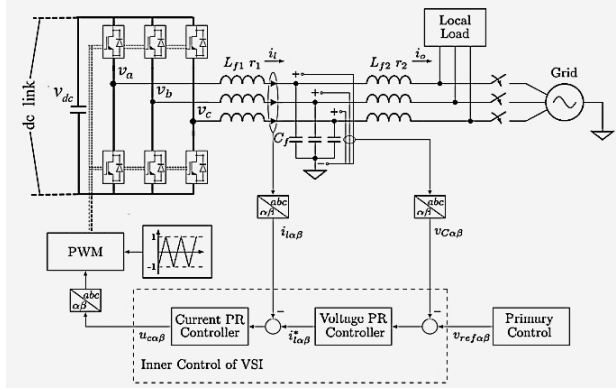
The zero level called the inner control is dedicated to cascading voltage and current control of VSI via the capacitor voltage and inductance current respectively as depicted in Fig 3. The proportional resonant (PR) controllers are adopted for both control loops. The transfer function of the PR controller is given as:

$$G_{PR}(s) = k_p + \frac{k_r s}{s^2 + \omega_c s + \omega_0^2} + \sum_{h=3,5,7} \frac{k_h s}{s^2 + h\omega_c s + (h\omega_0)^2} \quad (10)$$

where  $k_p$  is the proportional gain,  $k_h$  is the resonant gains at the h-harmonic,  $\omega_0$  and  $\omega_c$  represent the fundamental frequency and the resonance bandwidth.

This control is accomplished by using Clarke transformation to convert three phase system ( $abc$ ) into two independent single-phase system ( $\alpha\beta$ ), (see [4]).

An optimization algorithm is used to obtain the primary control parameters as well as the inner control ones.



**Fig. 3.** Schematic diagram of the zero-level control of the DG.

## 2.2 Secondary centralized control

The frequency and voltage magnitude deviations from their rated values that occur at the PCC are a consequence of the droop control characteristics. The secondary control is required to compensate these deviations. The expressions of both restoration compensators based on the PI-type controller are expressed as follow.

$$\delta\omega_{res} = k_{p\omega}(\omega_{pcc}^* - \omega_{pcc}) + k_{i\omega} \int (\omega_{pcc}^* - \omega_{pcc}) dt \quad (11)$$

$$\delta E_{res} = k_{pE}(E_{pcc}^* - V_{pcc}) + k_{iE} \int (E_{pcc}^* - V_{pcc}) dt \quad (12)$$

where  $k_{p\omega}$ ,  $k_{pE}$  are the proportional restoration controllers parameters,  $k_{i\omega}$  and  $k_{iE}$  are their integral ones.  $\omega_{pcc}$  is the frequency of common coupling (PCC) voltage.

Moreover, a third control loop is included within the secondary control scope when the grid connection mode is expected. It synchronizes the microgrid with the main grid for a smooth transition by reducing the phase shift between their voltages. Then, an amount of frequency  $\omega_s$  is sent to each VSI primary control through the secondary control.

The synchronization controller is given by using  $\alpha\beta$  components variables of the PCC and the grid voltages. For this end, the following equation must be satisfied:

$$\langle v_{pcc\alpha} v_{g\beta} - v_{pcc\beta} v_{g\alpha} \rangle = 0 \quad (13)$$

PI controller  $G_{syn}$  dedicated for synchronization control loop can be integrated as:

$$\omega_s = (v_{pcc\alpha} v_{g\beta} - v_{pcc\beta} v_{g\alpha}) G_{LPF}(s) G_{syn}(s) \quad (14)$$

Where

$$G_{syn}(s) = \frac{k_p s + k_i}{s} \quad (15)$$

$$G_{LPF}(s) = \frac{\omega_{LPF}}{\omega_{LPF} + s} \quad (16)$$

$k_p$  and  $k_i$  are the PI coefficients,  $\omega_s$  is the output of the synchronization loop.

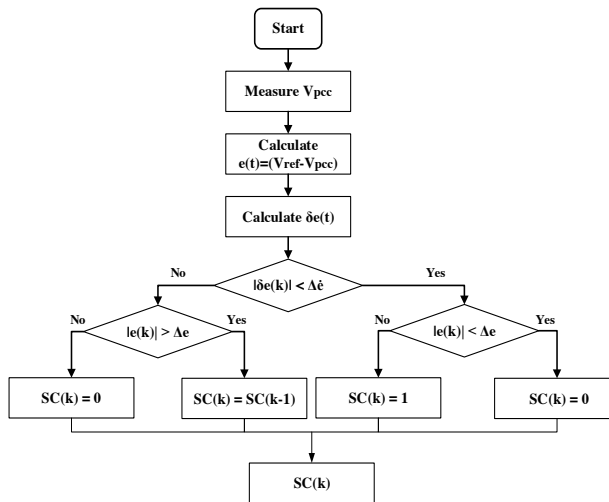
$G_{LPF}$  is a low-pass filter which is used for low bandwidth communications to all VSIs operate in parallel,  $\omega_{LPF}$  is its frequency and is selected as  $\omega_0/10$ .

### 2.3 The proposed tertiary level

The Microgrid concept has been proposed for flexible and efficient utilization of DGs. Then, with the increasing penetration of distributed generation, the modern control and management techniques are becoming increasingly attractive, as they offer higher flexibility and lower implementation cost [8]. This section deals with the development of a management framework dedicated to the tertiary level in order to make the secondary controller loops operate autonomously, as well as the switch (SS). We present a simple sequential logic approach that can be easily implemented. The operating principle of this approach is the combination of the sequential binary logic outputs: SC, SYN and ss which are used to On/Off the restoration loop, the synchronization control and the SS switching, respectively.

Let consider that  $e$  is the error between the PCC rated and the reference voltage ( $e = V_{ref} - V_{pcc}$ ),  $\delta e$  is its variation ( $\delta e = de/dt$ ) and  $k$  a time instant.

It is known that to ensure the global system stability, the primary control dynamic must be faster than the secondary control one. The secondary control is responsible for eliminating any steady state error  $e$  caused by the droop control. Indeed, the restoration loop is activated only when the tracking error becomes a non-null constant and its variation takes a very small value. However, this loop is deactivated just in the case when tracking error converges. The synchronization process can work only when the restoration loop is out of order. That is what ensure higher power quality compared with [4] during the transition from islanded to grid-connected mode. For these purposes, the following strategy is proposed in a tertiary level.



**Fig. 4.** Flow chart for SC signal in the proposed tertiary control strategy.

The decision variables in the time instant  $k$  are expressed as follow, respectively for On/Off of the restoration loop, the synchronization control and the SS switching.

$$SC(k) = \begin{cases} SC(k-1) & \text{if } |\delta e(k)| > \Delta \delta e \text{ AND } |e(k)| > \Delta e \\ 1 & \text{if } |e(k)| > \Delta e \\ 0 & \text{if } \text{else} \end{cases} \quad (17)$$

$$SYN(k) = \begin{cases} 1 & \text{if } g_c = 1 \text{ AND } SC = 0 \\ 0 & \text{if } g_c = 0 \text{ AND } SC = 1 \\ SYN(k-1) & \text{if } \text{else} \end{cases} \quad (18)$$

$$ss(k) = \overline{SC} * \overline{\Phi} * g_c ; \text{ Where } \Phi = \begin{cases} 0 & \text{if } |\varphi| < \Delta\varphi \\ 1 & \text{if } \text{else} \end{cases} \quad (19)$$

$\varphi$  is the phase difference between the PCC voltage and the grid voltage.  $g_c$  is binary signal expressing the intention of grid-disconnection ( $g_c = 0$ ) or grid-connection ( $g_c = 1$ ).  $\Delta e$ ,  $\Delta \dot{e}$  and  $\Delta \varphi$  are very small values of  $e$ ,  $\delta e$  and  $\varphi$ , respectively and  $*$  is the logical product operator.

The proposed tertiary level strategy algorithm for the restoration loop is illustrated through the flow chart shown in Fig. 4.

### 3 Optimal control parameters-tuning

Optimal parameters of the hierarchical control are calculated by using the metaheuristic so called Self learning particle swarm optimizer (SLPSO) algorithm [9], which is based on the minimization of a fitness function.

The SLPSO is an improved optimization structure of the classical PSO through learning techniques that are introduced for each particle  $k$  by using the following four operators, respectively:

- Operator 1: learning from its individual best particle ( $p_{best}$ ) position

$$\textit{Exploitation} : \mathbf{v}_k^d = \omega \mathbf{v}_k^d + \eta \mathbf{r}_k^d (\mathbf{pbest}_k^d - \mathbf{x}_k^d) \quad (20)$$

- Operator 2: learning from a random position nearby

$$\textit{Jumping out} : \mathbf{x}_k^d = \mathbf{x}_k^d + \mathbf{v}_{avg}^d \cdot N(0,1) \quad (21)$$

- Operator 3: learning from the  $p_{best}$  of a random particle

$$\textit{Exploration} : \mathbf{v}_k^d = \omega \mathbf{v}_k^d + \eta \mathbf{r}_k^d (\mathbf{pbest}_{k_{nearest}}^d - \mathbf{x}_k^d) \quad (22)$$

- Operator 4: learning from the global best particle archive ( $a_{best}$ ) position

$$\textit{Convergence} : \mathbf{v}_k^d = \omega \mathbf{v}_k^d + \eta \mathbf{r}_k^d (\mathbf{abest}^d - \mathbf{x}_k^d) \quad (23)$$

The PR parameters vector of the inner control is given by:

$$\boldsymbol{\theta} = [\omega_c, k_{pv}, k_{rv}, k_{3v}, k_{5v}, k_{7v}, k_{pi}, k_{ri}, k_{3i}, k_{5i}, k_{7i}]^T$$

The proposed fitness function is expressed as follow:

$$F_{PR}(\boldsymbol{\theta}) = \sum_{t=0}^{\infty} \left( (v_{refa}^t - v_{ca}^t(\boldsymbol{\theta}))^2 + (v_{refb}^t - v_{cb}^t(\boldsymbol{\theta}))^2 + (v_{refc}^t - v_{cc}^t(\boldsymbol{\theta}))^2 \right) \quad (24)$$

In order to increase the performance of the proposed droop control and secondary control, another fitness function is defined, to optimize all of their control parameters, as [4]:

$$F(\boldsymbol{\theta}) = \sum_{t=0}^{\infty} t |e_t(\boldsymbol{\theta})| [1 + \lambda - \lambda \text{sign}(e_t(\boldsymbol{\theta}))] \quad (25)$$

Being  $e_t(\theta)$  the difference between setpoint and real value by using  $\theta$  and  $\lambda$  is a constant coefficient that penalizes the oscillations.

In islanded mode,  $\theta_1^1 = [K_e, k_{dP}, k_{dQ}]^T$  is the parameters vector of the classical droop control and  $\theta_1^2 = [K_e, k_{fdP}, k_{fdQ}, \mu_1, \mu_2]^T$  is the parameters vector of the proposed droop control. In grid connected mode, both droop controls need the optimal of  $\theta_2 = [n_g, m_g]^T$ . The PI controller parameters vector of each secondary control loop is given by  $\theta = [k_p, k_i]^T$ . The optimal parameters of the global control of the system presented in section 4 are shown in Table 1, with  $\lambda = 50$ ,  $\Delta e = 0.2V$ ,  $\Delta \dot{e} = 4V/s$ ,  $N = 2$  (Oustaloup filter order). and  $[\omega_b, \omega_h] = [10^{-2}, 10^3]$ .

**Table 1.** Hierarchical control system parameters.

Inner control							
	$\omega_c$	$k_p$	$k_r$	$k_3$	$k_5$	$k_7$	
$G_{PR_v}$	0.0016	0.25	200.94	26.3	22.56	67.11	
$G_{PR_i}$	0.0016	0.1925	221.02	40.29	98.17	61.04	
Classical droop control ( $\mu_1 = \mu_2 = 1$ )							
	$K_e$	$k_{pP}$	$k_{pQ}$	$k_{dP}$	$k_{dQ}$	$n_g$	$m_g$
$VSI_1$	11.6	0.2890	$2.5 \times 10^{-4}$	0.0019	$2.8 \times 10^{-6}$	0.03	5.1
$VSI_2$	11.6	0.1089	$1.6 \times 10^{-4}$	0.0039	$3.3 \times 10^{-6}$	0.03	5.1
$VSI_3$	11.6	0.0871	$1.3 \times 10^{-4}$	0.0046	$1.7 \times 10^{-6}$	0.03	5.1
Fractional order droop control							
	$K_e$	$k_{fpP}$	$k_{fpQ}$	$k_{fdP}$	$k_{fdQ}$	$\mu_1$	$\mu_2$
$VSI_1$	13	0.3222	$2.5 \times 10^{-4}$	0.0025	$7.18 \times 10^{-7}$	1.135	1.35
$VSI_2$	13	0.2014	$1.6 \times 10^{-4}$	0.0014	$9.05 \times 10^{-6}$	1.154	0.88
$VSI_3$	13	0.1611	$1.3 \times 10^{-4}$	0.0038	$7.89 \times 10^{-6}$	0.961	0.97
Secondary control							
	Voltage loop		Frequency loop		Synchronization		
$k_p$	1.8815		2.2586		3.8		
$k_i$	4.2972		7.708		0		

## 4 Simulation Results

In order to test the feasibility of the proposed four levels hierarchical control, simulations are performed by using FOMCON Toolbox [10], a simulation Microgrid setup was built as depicted in Fig. 1, with the hierarchical control system and physical parameters given in Table 1 and Table 2, respectively.

**Table 2.** Physical parameters.

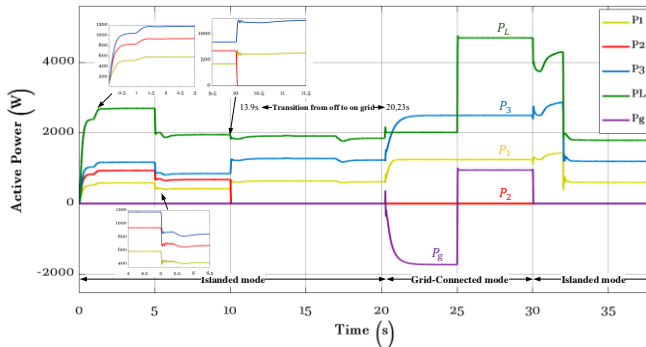
Electrical system parameters			
parameters	Symbol	Value	Unit
Rated voltage	$E^*$	220	V
Nominal frequency	$\omega^*$	$2\pi 50$	rad/s
Load inductance	$L_l$	84	$\mu H$
Load capacitance	$C_l$	500	$\mu C$
Load	$R_l$	100/140/145/60/150	$\Omega$



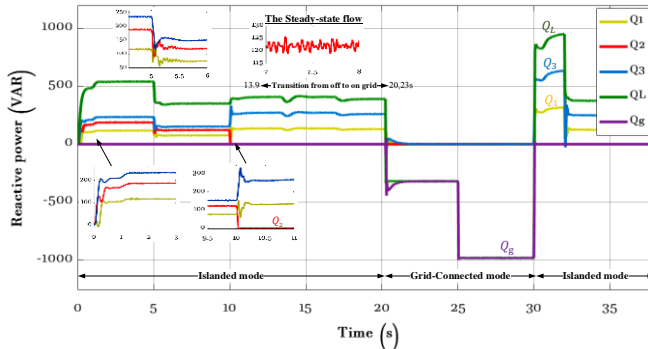
**VSIs parameters**

DC voltage	$V_{dc}$	650	V
Filter inductor	$L_{lf1,2}; r_{l1,2}$	1.8; 0.03	mH; $\Omega$
Filter capacitor	$C_{lf1,2}$	35	$\mu C$
PWM frequency	$f_s$	10	kHz
Output impedance	$Z_o$	$Z_{o1}$ : 2.8; 0.7 $Z_{o2}$ : 1.7; 0.5 $Z_{o3}$ : 1.6; 0.8	mH; $\Omega$
Apparent power rating	$S$	1250/2000/2500	kVA

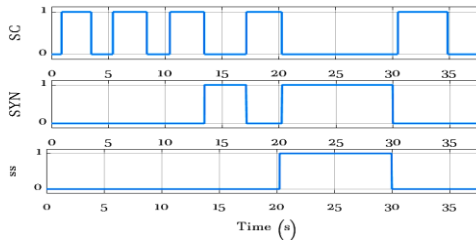
The test microgrid consists of three parallel DG units each one is composed of VSI and LCL filter, and a nonlinear load, connected between them through line impedance  $Z$ .



(a)



(b)

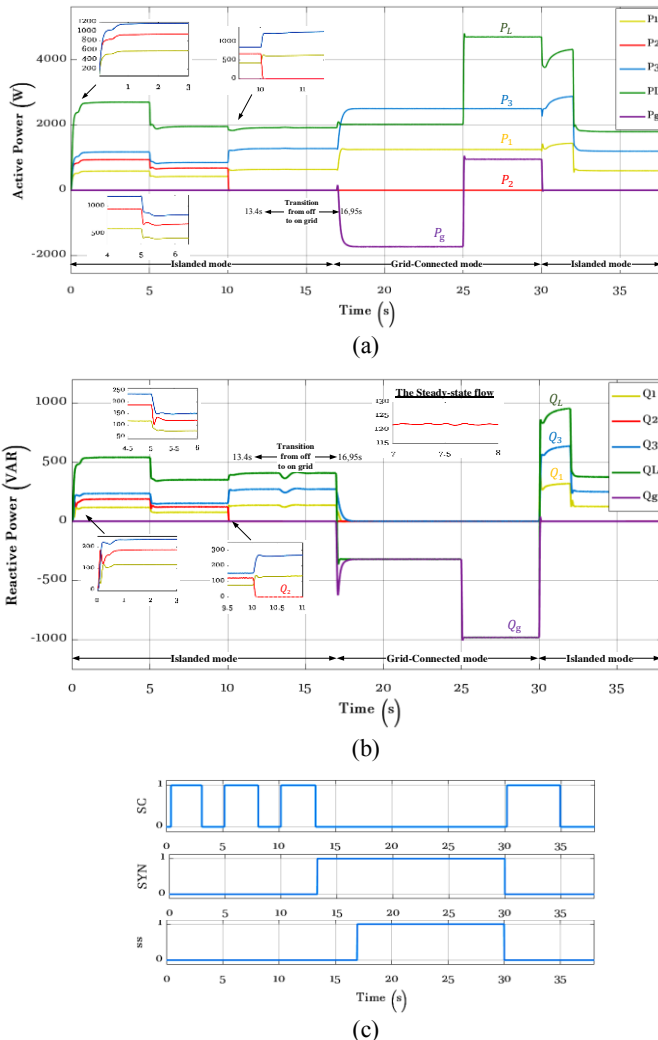


(c)

**Fig. 5.** Simulation results of Primary control and Tertiary level strategy scheme using the classical Droop Control (a) Active power; (b) Reactive power; (c) {SC; SYN; ss}.

In order to validate the improved droop control presented in this work, as well as the tertiary level strategy, different scenarios are simulated. After the operation start of the microgrid, the load demand is increased at  $t=5s$  which requires more power supply from the three connected DGs. The disconnection of the second DG (VSI2), at  $t=10s$  is also simulated. For a smooth transition from islanded mode to grid connected mode, the binary signal  $gc$  is transmitted to the tertiary control at  $t=12s$  to activate the synchronization process in order to eliminate the phase error between the PCC and main grid voltages. However, by according the strategy proposed in tertiary level, the synchronization process only works when the PCC voltage is restored, at  $t=13.9s$  by using the classical droop control and at  $t=13.4s$  by using the order-fractional one, as shown in Fig.5. and Fig.6.

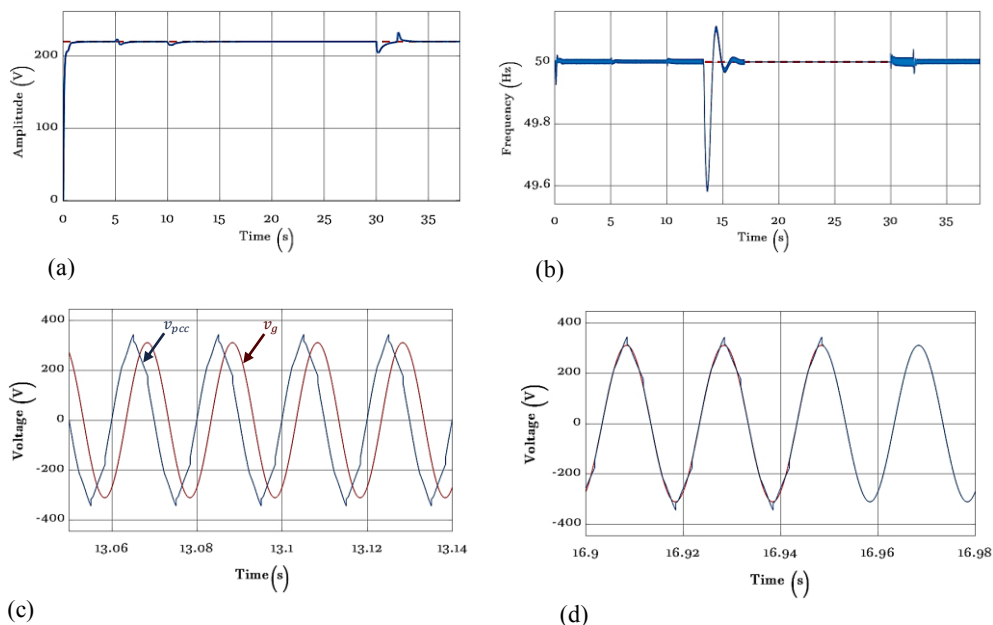
In Fig.5. it is shown that by using the classical droop control, another load variation test is simulated at  $t=17s$ , which makes the synchronization loop out of order, to complete the restoration of the PCC voltage. While, the non-integer order droop control, thanks to its rapidity compared with the classical one, allows the microgrid to connect to the main grid before load variation at  $t=16.95s$  (see Fig.5 and Fig.6).



**Fig. 6.** Simulation results of Primary control and Tertiary level strategy scheme using the Fractional-Order Droop Control (a) Active power; (b) Reactive power; (c) {SC; SYN; ss}.

According to Fig.5, Fig.6 and Fig.7, the simulation results demonstrate that, during each transient state, the proposed primary control with a fractional order derivative performs better than the one with the integer order in terms of a time response, overshoot and oscillations during steady-state flow, namely for the reactive power.

The performance of the binary sequential management strategy proposed for the tertiary level is illustrated via Fig.5(c) and Fig.6(c). This strategy proves its efficiency to make the secondary controller loops work autonomously, as well as the switch (SS). The restoration controller is started only when the droop control outputs are in steady state. Also, for a smooth transition to the connected-grid mode, the synchronization loop doesn't work until the restoration process is not completed. The switch SS is activated once the PCC and the main grid voltages are synchronized as shown in Fig.7. (d).



**Fig. 7.** Simulation results of Secondary control using the Fractional-Order Droop Control (a) PCC voltage amplitude; (b) Frequency; (c) and (d) The synchronization process between PCC and main grid voltage

## 5 Conclusion

In this paper, a four levels hierarchical control structure with a fractional order droop control is proposed for a three DGs flexible microgrid. The first level control which is called the primary control is based on an improved universal droop control developed in [4] by introducing a fractional order derivative operator. The output signal of the primary controller serves as a reference voltage for the inner controller (zero level) which is dedicated to cascading voltage and current control of VSI via the capacitor voltage and inductance current, respectively. In the secondary control, the magnitude and the frequency restorations loops are presented to compensate the deviations caused by the droop control loop. Also, this level includes the synchronization control loop. Most of control parameters are calculated by using the self-learning particle swarm optimizer (SLPSO) algorithm. A tertiary level is added in order to ensure higher flexibility of the microgrid and the power quality during transition mode. In this last level, a sequential logical strategy is proposed to ensure smooth

transition between different modes of operation. Simulations are performed to highlight the performances of the proposed control scheme compared with the known three level hierarchical one.

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